

## Data Modeling Using the Entity–Relationship (ER) Model

Conceptual modeling is a very important phase in designing a successful database application. Generally, the term **database application** refers to a particular database and the associated programs that implement the database queries and updates. For example, a BANK database application that keeps track of customer accounts would include programs that implement database updates corresponding to customer deposits and withdrawals. These programs would provide user-friendly graphical user interfaces (GUIs) utilizing forms and menus for the end users of the application—the bank customers or bank tellers in this example. In addition, it is now common to provide interfaces to these programs to BANK customers via mobile devices using **mobile apps**. Hence, a major part of the database application will require the design, implementation, and testing of these application programs. Traditionally, the design and testing of **application programs** has been considered to be part of *software engineering* rather than *database design*. In many software design tools, the database design methodologies and software engineering methodologies are intertwined since these activities are strongly related.

In this chapter, we follow the traditional approach of concentrating on the database structures and constraints during conceptual database design. The design of application programs is typically covered in software engineering courses. We present the modeling concepts of the **entity–relationship (ER) model**, which is a popular high-level conceptual data model. This model and its variations are frequently used for the conceptual design of database applications, and many database design tools employ its concepts. We describe the basic data-structuring concepts and constraints of the ER model and discuss their use in the design of conceptual schemas for database applications. We also present the diagrammatic notation associated with the ER model, known as **ER diagrams**.

Object modeling methodologies such as the **Unified Modeling Language (UML)** are becoming increasingly popular in both database and software design. These methodologies go beyond database design to specify detailed design of software modules and their interactions using various types of diagrams. An important part of these methodologies—namely, *class diagrams*<sup>1</sup>—is similar in many ways to the ER diagrams. In class diagrams, *operations* on objects are specified, in addition to specifying the database schema structure. Operations can be used to specify the *functional requirements* during database design, as we will discuss in Section 3.1. We present some of the UML notation and concepts for class diagrams that are particularly relevant to database design in Section 3.8, and we briefly compare these to ER notation and concepts. Additional UML notation and concepts are presented in Section 4.6.

This chapter is organized as follows: Section 3.1 discusses the role of high-level conceptual data models in database design. We introduce the requirements for a sample database application in Section 3.2 to illustrate the use of concepts from the ER model. This sample database is used throughout the text. In Section 3.3 we present the concepts of entities and attributes, and we gradually introduce the diagrammatic technique for displaying an ER schema. In Section 3.4 we introduce the concepts of binary relationships and their roles and structural constraints. Section 3.5 introduces weak entity types. Section 3.6 shows how a schema design is refined to include relationships. Section 3.7 reviews the notation for ER diagrams, summarizes the issues and common pitfalls that occur in schema design, and discusses how to choose the names for database schema constructs such as entity types and relationship types. Section 3.8 introduces some UML class diagram concepts, compares them to ER model concepts, and applies them to the same COMPANY database example. Section 3.9 discusses more complex types of relationships. Section 3.10 summarizes the chapter.

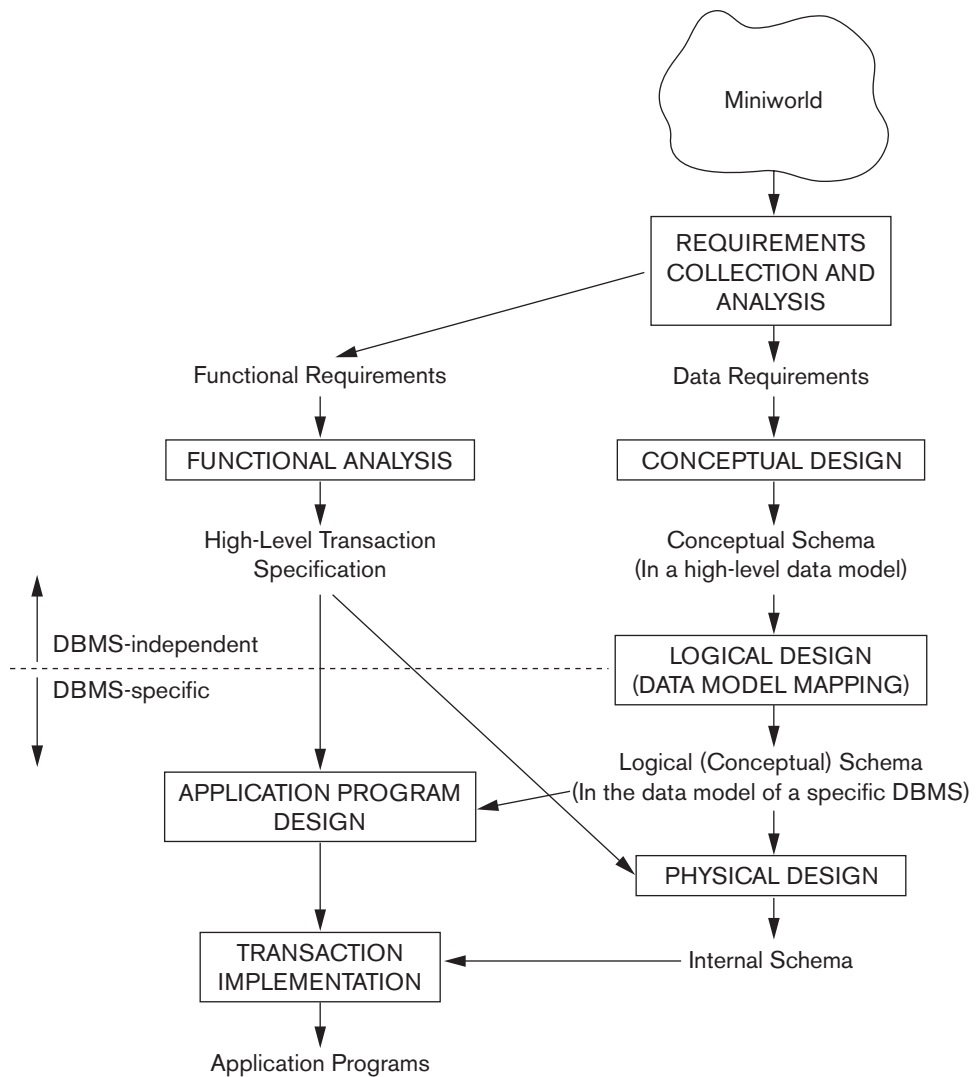
The material in Sections 3.8 and 3.9 may be excluded from an introductory course. If a more thorough coverage of data modeling concepts and conceptual database design is desired, the reader should continue to Chapter 4, where we describe extensions to the ER model that lead to the enhanced-ER (EER) model, which includes concepts such as specialization, generalization, inheritance, and union types (categories).

## 3.1 Using High-Level Conceptual Data Models for Database Design

Figure 3.1 shows a simplified overview of the database design process. The first step shown is **requirements collection and analysis**. During this step, the database designers interview prospective database users to understand and document their **data requirements**. The result of this step is a concisely written set of users' requirements. These requirements should be specified in as detailed and complete a form as possible. In parallel with specifying the data requirements, it is useful to specify

---

<sup>1</sup>A **class** is similar to an *entity type* in many ways.



**Figure 3.1**  
A simplified diagram to illustrate the main phases of database design.

the known **functional requirements** of the application. These consist of the user-defined **operations** (or **transactions**) that will be applied to the database, including both retrievals and updates. In software design, it is common to use *data flow diagrams*, *sequence diagrams*, *scenarios*, and other techniques to specify functional requirements. We will not discuss any of these techniques here; they are usually described in detail in software engineering texts.

Once the requirements have been collected and analyzed, the next step is to create a **conceptual schema** for the database, using a high-level conceptual data model. This

step is called **conceptual design**. The conceptual schema is a concise description of the data requirements of the users and includes detailed descriptions of the entity types, relationships, and constraints; these are expressed using the concepts provided by the high-level data model. Because these concepts do not include implementation details, they are usually easier to understand and can be used to communicate with nontechnical users. The high-level conceptual schema can also be used as a reference to ensure that all users' data requirements are met and that the requirements do not conflict. This approach enables database designers to concentrate on specifying the properties of the data, without being concerned with storage and implementation details, which makes it easier to create a good conceptual database design.

During or after the conceptual schema design, the basic data model operations can be used to specify the high-level user queries and operations identified during functional analysis. This also serves to confirm that the conceptual schema meets all the identified functional requirements. Modifications to the conceptual schema can be introduced if some functional requirements cannot be specified using the initial schema.

The next step in database design is the actual implementation of the database, using a commercial DBMS. Most current commercial DBMSs use an implementation data model—such as the relational (SQL) model—so the conceptual schema is transformed from the high-level data model into the implementation data model. This step is called **logical design** or **data model mapping**; its result is a database schema in the implementation data model of the DBMS. Data model mapping is often automated or semiautomated within the database design tools.

The last step is the **physical design** phase, during which the internal storage structures, file organizations, indexes, access paths, and physical design parameters for the database files are specified. In parallel with these activities, application programs are designed and implemented as database transactions corresponding to the high-level transaction specifications.

We present only the basic ER model concepts for conceptual schema design in this chapter. Additional modeling concepts are discussed in Chapter 4, when we introduce the EER model.

## 3.2 A Sample Database Application

In this section we describe a sample database application, called COMPANY, which serves to illustrate the basic ER model concepts and their use in schema design. We list the data requirements for the database here, and then create its conceptual schema step-by-step as we introduce the modeling concepts of the ER model. The COMPANY database keeps track of a company's employees, departments, and projects. Suppose that after the requirements collection and analysis phase, the database designers provide the following description of the *miniworld*—the part of the company that will be represented in the database.

- The company is organized into departments. Each department has a unique name, a unique number, and a particular employee who manages the department. We keep track of the start date when that employee began managing the department. A department may have several locations.
- A department controls a number of projects, each of which has a unique name, a unique number, and a single location.
- The database will store each employee's name, Social Security number,<sup>2</sup> address, salary, sex (gender), and birth date. An employee is assigned to one department, but may work on several projects, which are not necessarily controlled by the same department. It is required to keep track of the current number of hours per week that an employee works on each project, as well as the direct supervisor of each employee (who is another employee).
- The database will keep track of the dependents of each employee for insurance purposes, including each dependent's first name, sex, birth date, and relationship to the employee.

Figure 3.2 shows how the schema for this database application can be displayed by means of the graphical notation known as **ER diagrams**. This figure will be explained gradually as the ER model concepts are presented. We describe the step-by-step process of deriving this schema from the stated requirements—and explain the ER diagrammatic notation—as we introduce the ER model concepts.

## 3.3 Entity Types, Entity Sets, Attributes, and Keys

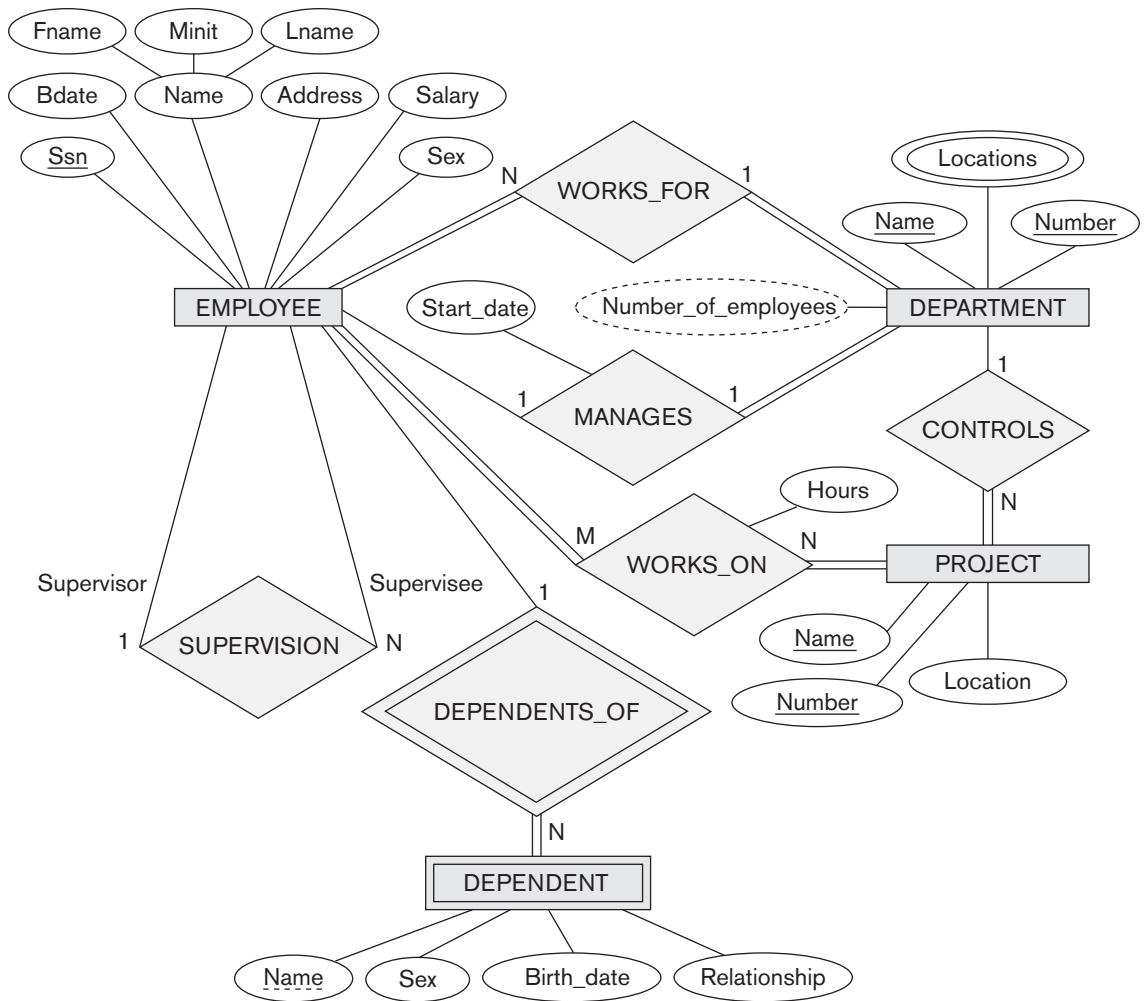
The ER model describes data as *entities*, *relationships*, and *attributes*. In Section 3.3.1 we introduce the concepts of entities and their attributes. We discuss entity types and key attributes in Section 3.3.2. Then, in Section 3.3.3, we specify the initial conceptual design of the entity types for the COMPANY database. We describe relationships in Section 3.4.

### 3.3.1 Entities and Attributes

**Entities and Their Attributes.** The basic concept that the ER model represents is an **entity**, which is a *thing* or *object* in the real world with an independent existence. An entity may be an object with a physical existence (for example, a particular person, car, house, or employee) or it may be an object with a conceptual existence (for instance, a company, a job, or a university course). Each entity has **attributes**—the particular properties that describe it. For example, an EMPLOYEE entity may be described by the employee's name, age, address, salary, and job. A particular entity

---

<sup>2</sup>The Social Security number, or SSN, is a unique nine-digit identifier assigned to each individual in the United States to keep track of his or her employment, benefits, and taxes. Other countries may have similar identification schemes, such as personal identification card numbers.

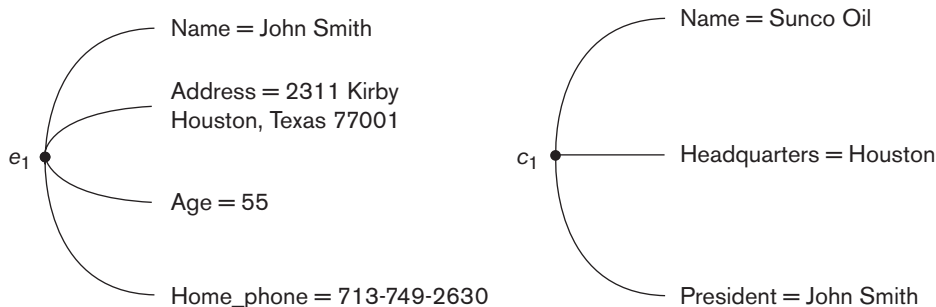


**Figure 3.2**

An ER schema diagram for the COMPANY database. The diagrammatic notation is introduced gradually throughout this chapter and is summarized in Figure 3.14.

will have a value for each of its attributes. The attribute values that describe each entity become a major part of the data stored in the database.

Figure 3.3 shows two entities and the values of their attributes. The EMPLOYEE entity  $e_1$  has four attributes: Name, Address, Age, and Home\_phone; their values are 'John Smith,' '2311 Kirby, Houston, Texas 77001', '55', and '713-749-2630', respectively. The COMPANY entity  $c_1$  has three attributes: Name, Headquarters, and President; their values are 'Sunco Oil', 'Houston', and 'John Smith', respectively.

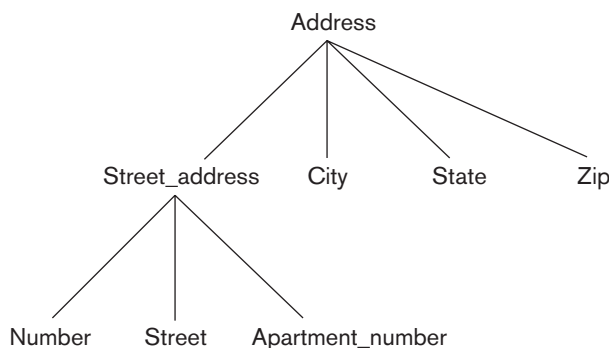


**Figure 3.3**  
Two entities, EMPLOYEE  $e_1$ , COMPANY  $c_1$ , their attributes.

Several types of attributes occur in the ER model: *simple* versus *composite*, *single-valued* versus *multivalued*, and *stored* versus *derived*. First we define these attribute types and illustrate their use via examples. Then we discuss the concept of a *NULL value* for an attribute.

**Composite versus Simple (Atomic) Attributes.** **Composite attributes** can be divided into smaller subparts, which represent more basic attributes with independent meanings. For example, the Address attribute of the EMPLOYEE entity shown in Figure 3.3 can be subdivided into Street\_address, City, State, and Zip,<sup>3</sup> with the values ‘2311 Kirby’, ‘Houston’, ‘Texas’, and ‘77001’. Attributes that are not divisible are called **simple** or **atomic attributes**. Composite attributes can form a hierarchy; for example, Street\_address can be further subdivided into three simple component attributes: Number, Street, and Apartment\_number, as shown in Figure 3.4. The value of a composite attribute is the concatenation of the values of its component simple attributes.

Composite attributes are useful to model situations in which a user sometimes refers to the composite attribute as a unit but at other times refers specifically to its



**Figure 3.4**  
A hierarchy of composite attributes.

<sup>3</sup>Zip Code is the name used in the United States for a five-digit postal code, such as 76019, which can be extended to nine digits, such as 76019-0015. We use the five-digit Zip in our examples.

components. If the composite attribute is referenced only as a whole, there is no need to subdivide it into component attributes. For example, if there is no need to refer to the individual components of an address (Zip Code, street, and so on), then the whole address can be designated as a simple attribute.

**Single-Valued versus Multivalued Attributes.** Most attributes have a single value for a particular entity; such attributes are called **single-valued**. For example, Age is a single-valued attribute of a person. In some cases an attribute can have a set of values for the same entity—for instance, a Colors attribute for a car, or a College\_degrees attribute for a person. Cars with one color have a single value, whereas two-tone cars have two color values. Similarly, one person may not have any college degrees, another person may have one, and a third person may have two or more degrees; therefore, different people can have different *numbers of values* for the College\_degrees attribute. Such attributes are called **multivalued**. A multivalued attribute may have lower and upper bounds to constrain the *number of values* allowed for each individual entity. For example, the Colors attribute of a car may be restricted to have between one and two values, if we assume that a car can have two colors at most.

**Stored versus Derived Attributes.** In some cases, two (or more) attribute values are related—for example, the Age and Birth\_date attributes of a person. For a particular person entity, the value of Age can be determined from the current (today's) date and the value of that person's Birth\_date. The Age attribute is hence called a **derived attribute** and is said to be **derivable from** the Birth\_date attribute, which is called a **stored attribute**. Some attribute values can be derived from *related entities*; for example, an attribute Number\_of\_employees of a DEPARTMENT entity can be derived by counting the number of employees related to (working for) that department.

**NULL Values.** In some cases, a particular entity may not have an applicable value for an attribute. For example, the Apartment\_number attribute of an address applies only to addresses that are in apartment buildings and not to other types of residences, such as single-family homes. Similarly, a College\_degrees attribute applies only to people with college degrees. For such situations, a special value called NULL is created. An address of a single-family home would have NULL for its Apartment\_number attribute, and a person with no college degree would have NULL for College\_degrees. NULL can also be used if we do not know the value of an attribute for a particular entity—for example, if we do not know the home phone number of 'John Smith' in Figure 3.3. The meaning of the former type of NULL is *not applicable*, whereas the meaning of the latter is *unknown*. The *unknown* category of NULL can be further classified into two cases. The first case arises when it is known that the attribute value exists but is *missing*—for instance, if the Height attribute of a person is listed as NULL. The second case arises when it is *not known* whether the attribute value exists—for example, if the Home\_phone attribute of a person is NULL.

**Complex Attributes.** Notice that, in general, composite and multivalued attributes can be nested arbitrarily. We can represent arbitrary nesting by grouping



```
{Address_phone( {Phone(Area_code,Phone_number)},Address(Street_address
(Number,Street,Apartment_number),City,State,Zip) )}
```

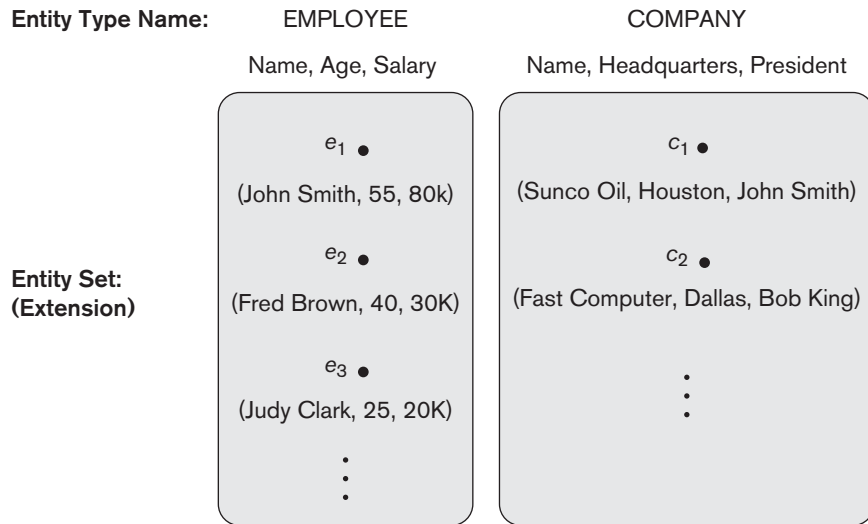
**Figure 3.5**

A complex attribute  
Address\_phone.

components of a composite attribute between parentheses ( ) and separating the components with commas, and by displaying multivalued attributes between braces { }. Such attributes are called **complex attributes**. For example, if a person can have more than one residence and each residence can have a single address and multiple phones, an attribute Address\_phone for a person can be specified as shown in Figure 3.5.<sup>4</sup> Both Phone and Address are themselves composite attributes.

### 3.3.2 Entity Types, Entity Sets, Keys, and Value Sets

**Entity Types and Entity Sets.** A database usually contains groups of entities that are similar. For example, a company employing hundreds of employees may want to store similar information concerning each of the employees. These employee entities share the same attributes, but each entity has its *own value(s)* for each attribute. An **entity type** defines a *collection (or set)* of entities that have the same attributes. Each entity type in the database is described by its name and attributes. Figure 3.6 shows two entity types: EMPLOYEE and COMPANY, and a list of some of the attributes for each. A few individual entities of each type are also illustrated, along with the values of their attributes. The collection of all entities of a particular entity type in the



**Figure 3.6**

Two entity types,  
EMPLOYEE and  
COMPANY, and so  
member entities of  
each.

<sup>4</sup>For those familiar with XML, we should note that complex attributes are similar to complex elements in XML (see Chapter 13).

database at any point in time is called an **entity set** or **entity collection**; the entity set is usually referred to using the same name as the entity type, even though they are two separate concepts. For example, EMPLOYEE refers to both a *type of entity* as well as the current collection of *all employee entities* in the database. It is now more common to give separate names to the entity type and entity collection; for example in object and object-relational data models (see Chapter 12).

An entity type is represented in ER diagrams<sup>5</sup> (see Figure 3.2) as a rectangular box enclosing the entity type name. Attribute names are enclosed in ovals and are attached to their entity type by straight lines. Composite attributes are attached to their component attributes by straight lines. Multivalued attributes are displayed in double ovals. Figure 3.7(a) shows a CAR entity type in this notation.

An entity type describes the **schema** or **intension** for a *set of entities* that share the same structure. The collection of entities of a particular entity type is grouped into an entity set, which is also called the **extension** of the entity type.

**Key Attributes of an Entity Type.** An important constraint on the entities of an entity type is the **key** or **uniqueness constraint** on attributes. An entity type usually has one or more attributes whose values are distinct for each individual entity in the entity set. Such an attribute is called a **key attribute**, and its values can be used to identify each entity uniquely. For example, the Name attribute is a key of the COMPANY entity type in Figure 3.6 because no two companies are allowed to have the same name. For the PERSON entity type, a typical key attribute is Ssn (Social Security number). Sometimes several attributes together form a key, meaning that the *combination* of the attribute values must be distinct for each entity. If a set of attributes possesses this property, the proper way to represent this in the ER model that we describe here is to define a *composite attribute* and designate it as a key attribute of the entity type. Notice that such a composite key must be *minimal*; that is, all component attributes must be included in the composite attribute to have the uniqueness property. Superfluous attributes must not be included in a key. In ER diagrammatic notation, each key attribute has its name **underlined** inside the oval, as illustrated in Figure 3.7(a).

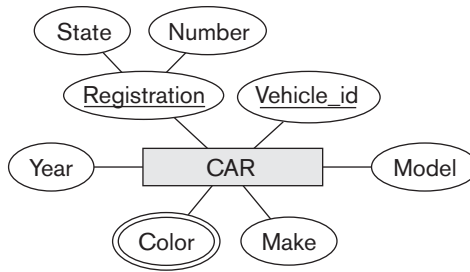
Specifying that an attribute is a key of an entity type means that the preceding uniqueness property must hold for *every entity set* of the entity type. Hence, it is a constraint that prohibits any two entities from having the same value for the key attribute at the same time. It is not the property of a particular entity set; rather, it is a constraint on *any entity set* of the entity type at any point in time. This key constraint (and other constraints we discuss later) is derived from the constraints of the miniworld that the database represents.

Some entity types have *more than one* key attribute. For example, each of the Vehicle\_id and Registration attributes of the entity type CAR (Figure 3.7) is a key in

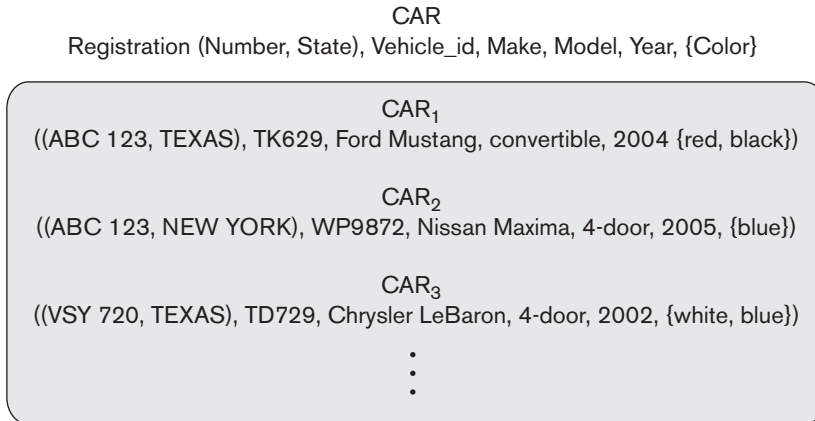
---

<sup>5</sup>We use a notation for ER diagrams that is close to the original proposed notation (Chen, 1976). Many other notations are in use; we illustrate some of them later in this chapter when we present UML class diagrams, and some additional diagrammatic notations are given in Appendix A.

(a)



(b)



**Figure 3.7**

The CAR entity type with two key attributes, Registration and Vehicle\_id. (a) ER diagram notation. (b) Entity set with three entities.

its own right. The Registration attribute is an example of a composite key formed from two simple component attributes, State and Number, neither of which is a key on its own. An entity type may also have *no key*, in which case it is called a *weak entity type* (see Section 3.5).

In our diagrammatic notation, if two attributes are underlined separately, then *each is a key on its own*. Unlike the relational model (see Section 5.2.2), there is no concept of primary key in the ER model that we present here; the primary key will be chosen during mapping to a relational schema (see Chapter 9).

**Value Sets (Domains) of Attributes.** Each simple attribute of an entity type is associated with a **value set** (or **domain** of values), which specifies the set of values that may be assigned to that attribute for each individual entity. In Figure 3.6, if the range of ages allowed for employees is between 16 and 70, we can specify the value set of the Age attribute of EMPLOYEE to be the set of integer numbers between 16 and 70. Similarly, we can specify the value set for the Name attribute to be the set of strings of alphabetic characters separated by blank characters, and so on. Value sets are not typically displayed in basic ER diagrams and are similar to the basic **data types** available in most programming languages, such as integer, string, Boolean, float, enumerated type, subrange, and so on. However, data types of attributes can

be specified in UML class diagrams (see Section 3.8) and in other diagrammatic notations used in database design tools. Additional data types to represent common database types, such as date, time, and other concepts, are also employed.

Mathematically, an attribute  $A$  of entity set  $E$  whose value set is  $V$  can be defined as a **function** from  $E$  to the power set<sup>6</sup>  $P(V)$  of  $V$ :

$$A : E \rightarrow P(V)$$

We refer to the value of attribute  $A$  for entity  $e$  as  $A(e)$ . The previous definition covers both single-valued and multivalued attributes, as well as NULLs. A NULL value is represented by the *empty set*. For single-valued attributes,  $A(e)$  is restricted to being a *singleton set* for each entity  $e$  in  $E$ , whereas there is no restriction on multivalued attributes.<sup>7</sup> For a composite attribute  $A$ , the value set  $V$  is the power set of the Cartesian product of  $P(V_1), P(V_2), \dots, P(V_n)$ , where  $V_1, V_2, \dots, V_n$  are the value sets of the simple component attributes that form  $A$ :

$$V = P(P(V_1) \times P(V_2) \times \dots \times P(V_n))$$

The value set provides all possible values. Usually only a small number of these values exist in the database at a particular time. Those values represent the data from the current state of the miniworld and correspond to the data as it actually exists in the miniworld.

### 3.3.3 Initial Conceptual Design of the COMPANY Database

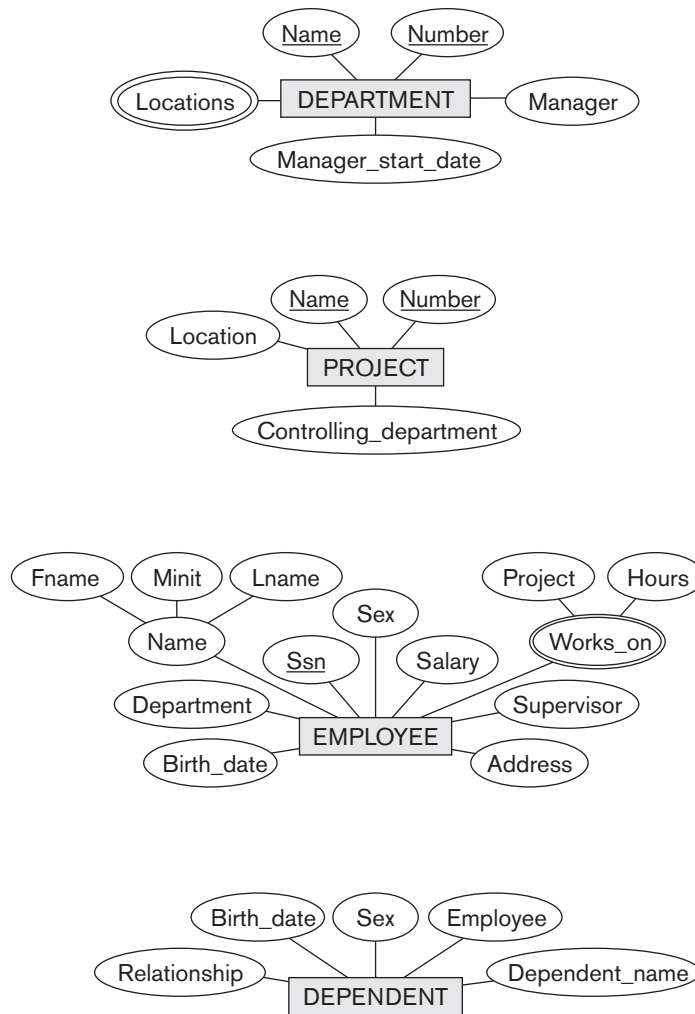
We can now define the entity types for the COMPANY database, based on the requirements described in Section 3.2. After defining several entity types and their attributes here, we refine our design in Section 3.4 after we introduce the concept of a relationship. According to the requirements listed in Section 3.2, we can identify four entity types—one corresponding to each of the four items in the specification (see Figure 3.8):

1. An entity type DEPARTMENT with attributes Name, Number, Locations, Manager, and Manager\_start\_date. Locations is the only multivalued attribute. We can specify that both Name and Number are (separate) key attributes because each was specified to be unique.
2. An entity type PROJECT with attributes Name, Number, Location, and Controlling\_department. Both Name and Number are (separate) key attributes.
3. An entity type EMPLOYEE with attributes Name, Ssn, Sex, Address, Salary, Birth\_date, Department, and Supervisor. Both Name and Address may be composite attributes; however, this was not specified in the requirements. We must go back to the users to see if any of them will refer to the individual components of Name—First\_name, Middle\_initial, Last\_name—or of Address. In

---

<sup>6</sup>The **power set**  $P(V)$  of a set  $V$  is the set of all subsets of  $V$ .

<sup>7</sup>A **singleton** set is a set with only one element (value).



**Figure 3.8**

Preliminary design entity types for the COMPANY database. Some of the shown attributes will be re into relationships.

our example, Name is modeled as a composite attribute, whereas Address is not, presumably after consultation with the users.

4. An entity type DEPENDENT with attributes Employee, Dependent\_name, Sex, Birth\_date, and Relationship (to the employee).

Another requirement is that an employee can work on several projects, and the database has to store the number of hours per week an employee works on each project. This requirement is listed as part of the third requirement in Section 3.2, and it can be represented by a multivalued composite attribute of EMPLOYEE called Works\_on with the simple components (Project, Hours). Alternatively, it can be represented as a multivalued composite attribute of PROJECT called Workers with the simple components (Employee, Hours). We choose the first

alternative in Figure 3.8; we shall see in the next section that this will be refined into a many-to-many relationship, once we introduce the concepts of relationships.

## 3.4 Relationship Types, Relationship Sets, Roles, and Structural Constraints

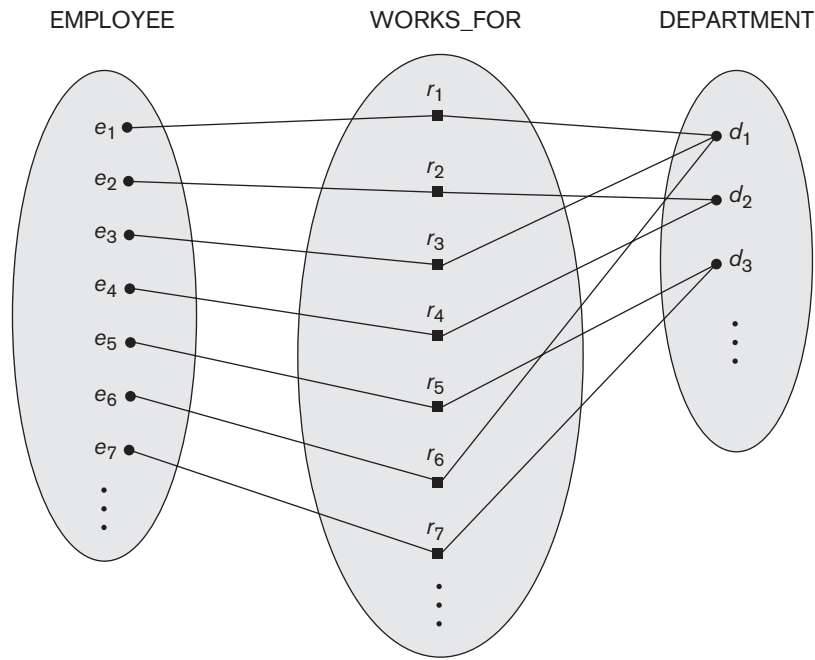
In Figure 3.8 there are several *implicit relationships* among the various entity types. In fact, whenever an attribute of one entity type refers to another entity type, some relationship exists. For example, the attribute `Manager` of `DEPARTMENT` refers to an employee who manages the department; the attribute `Controlling_department` of `PROJECT` refers to the department that controls the project; the attribute `Supervisor` of `EMPLOYEE` refers to another employee (the one who supervises this employee); the attribute `Department` of `EMPLOYEE` refers to the department for which the employee works; and so on. In the ER model, these references should not be represented as attributes but as **relationships**. The initial `COMPANY` database schema from Figure 3.8 will be refined in Section 3.6 to represent relationships explicitly. In the initial design of entity types, relationships are typically captured in the form of attributes. As the design is refined, these attributes get converted into relationships between entity types.

This section is organized as follows: Section 3.4.1 introduces the concepts of relationship types, relationship sets, and relationship instances. We define the concepts of relationship degree, role names, and recursive relationships in Section 3.4.2, and then we discuss structural constraints on relationships—such as cardinality ratios and existence dependencies—in Section 3.4.3. Section 3.4.4 shows how relationship types can also have attributes.

### 3.4.1 Relationship Types, Sets, and Instances

A **relationship type**  $R$  among  $n$  entity types  $E_1, E_2, \dots, E_n$  defines a set of associations—or a **relationship set**—among entities from these entity types. Similar to the case of entity types and entity sets, a relationship type and its corresponding relationship set are customarily referred to by the *same name*,  $R$ . Mathematically, the relationship set  $R$  is a set of **relationship instances**  $r_i$ , where each  $r_i$  associates  $n$  individual entities  $(e_1, e_2, \dots, e_n)$ , and each entity  $e_j$  in  $r_i$  is a member of entity set  $E_j$ ,  $1 \leq j \leq n$ . Hence, a relationship set is a mathematical relation on  $E_1, E_2, \dots, E_n$ ; alternatively, it can be defined as a subset of the Cartesian product of the entity sets  $E_1 \times E_2 \times \dots \times E_n$ . Each of the entity types  $E_1, E_2, \dots, E_n$  is said to **participate** in the relationship type  $R$ ; similarly, each of the individual entities  $e_1, e_2, \dots, e_n$  is said to **participate** in the relationship instance  $r_i = (e_1, e_2, \dots, e_n)$ .

Informally, each relationship instance  $r_i$  in  $R$  is an association of entities, where the association includes exactly one entity from each participating entity type. Each such relationship instance  $r_i$  represents the fact that the entities participating in  $r_i$  are related in some way in the corresponding miniworld situation. For example, consider a relationship type `WORKS_FOR` between the two entity types



**Figure 3.9**

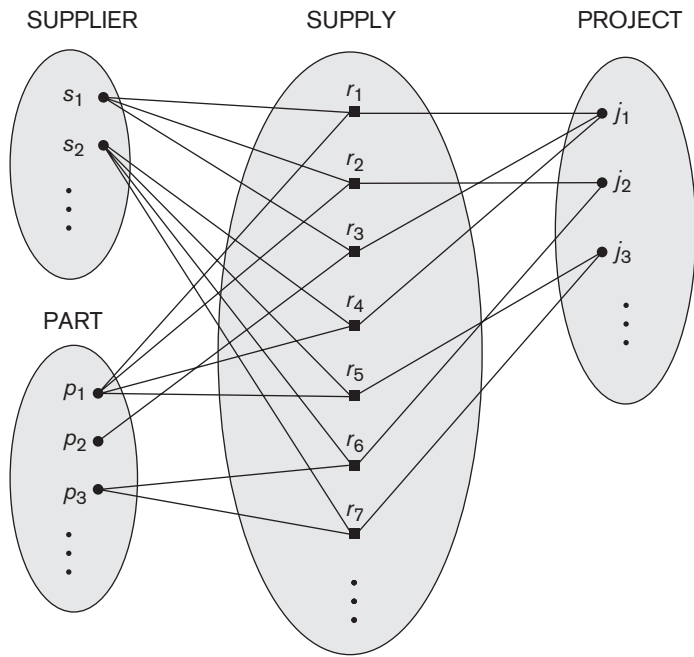
Some instances in the WORKS\_FOR relationship set, which represents a relationship type WORKS\_FOR between EMPLOYEE and DEPARTMENT.

EMPLOYEE and DEPARTMENT, which associates each employee with the department for which the employee works. Each relationship instance in the relationship set WORKS\_FOR associates one EMPLOYEE entity and one DEPARTMENT entity. Figure 3.9 illustrates this example, where each relationship instance  $r_i$  is shown connected to the EMPLOYEE and DEPARTMENT entities that participate in  $r_i$ . In the miniworld represented by Figure 3.9, the employees  $e_1, e_3$ , and  $e_6$  work for department  $d_1$ ; the employees  $e_2$  and  $e_4$  work for department  $d_2$ ; and the employees  $e_5$  and  $e_7$  work for department  $d_3$ .

In ER diagrams, relationship types are displayed as diamond-shaped boxes, which are connected by straight lines to the rectangular boxes representing the participating entity types. The relationship name is displayed in the diamond-shaped box (see Figure 3.2).

### 3.4.2 Relationship Degree, Role Names, and Recursive Relationships

**Degree of a Relationship Type.** The **degree** of a relationship type is the number of participating entity types. Hence, the WORKS\_FOR relationship is of degree two. A relationship type of degree two is called **binary**, and one of degree three is called **ternary**. An example of a ternary relationship is SUPPLY, shown in Figure 3.10, where each relationship instance  $r_i$  associates three entities—a supplier  $s$ , a part  $p$ , and a project  $j$ —whenever  $s$  supplies part  $p$  to project  $j$ . Relationships can



**Figure 3.10**  
Some relationship instances in the SUPPLY ternary relationship set.

generally be of any degree, but the ones most common are binary relationships. Higher-degree relationships are generally more complex than binary relationships; we characterize them further in Section 3.9.

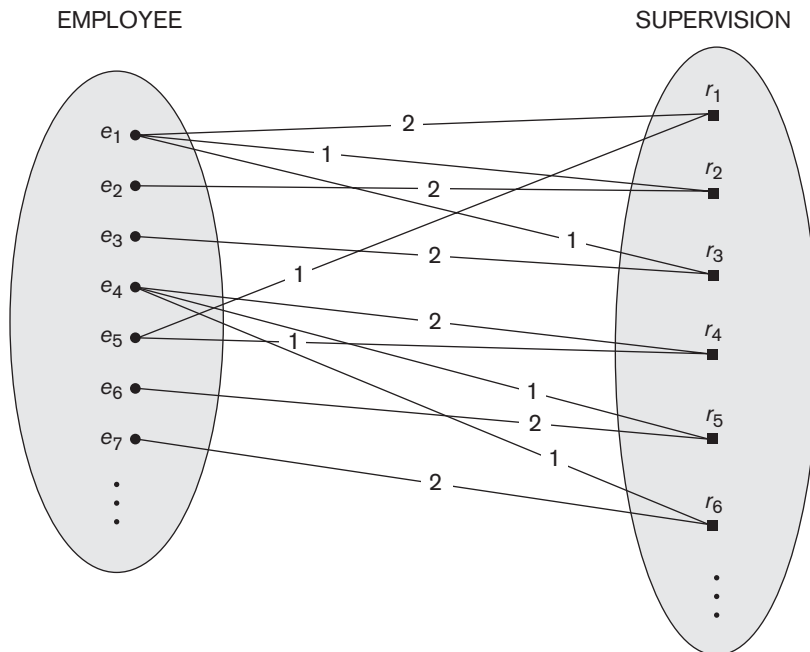
**Relationships as Attributes.** It is sometimes convenient to think of a binary relationship type in terms of attributes, as we discussed in Section 3.3.3. Consider the WORKS\_FOR relationship type in Figure 3.9. One can think of an attribute called Department of the EMPLOYEE entity type, where the value of Department for each EMPLOYEE entity is (a reference to) the DEPARTMENT entity for which that employee works. Hence, the value set for this Department attribute is the set of *all* DEPARTMENT entities, which is the DEPARTMENT entity set. This is what we did in Figure 3.8 when we specified the initial design of the entity type EMPLOYEE for the COMPANY database. However, when we think of a binary relationship as an attribute, we always have two options or two points of view. In this example, the alternative point of view is to think of a multivalued attribute Employees of the entity type DEPARTMENT whose value for each DEPARTMENT entity is the set of EMPLOYEE entities who work for that department. The value set of this Employees attribute is the power set of the EMPLOYEE entity set. Either of these two attributes—Department of EMPLOYEE or Employees of DEPARTMENT—can represent the WORKS\_FOR relationship type. If both are represented, they are constrained to be inverses of each other.<sup>8</sup>

<sup>8</sup>This concept of representing relationship types as attributes is used in a class of data models called **functional data models**. In object databases (see Chapter 12), relationships can be represented by reference attributes, either in one direction or in both directions as inverses. In relational databases (see Chapter 5), foreign keys are a type of reference attribute used to represent relationships.



**Role Names and Recursive Relationships.** Each entity type that participates in a relationship type plays a particular role in the relationship. The **role name** signifies the role that a participating entity from the entity type plays in each relationship instance, and it helps to explain what the relationship means. For example, in the WORKS\_FOR relationship type, EMPLOYEE plays the role of *employee* or *worker* and DEPARTMENT plays the role of *department* or *employer*.

Role names are not technically necessary in relationship types where all the participating entity types are distinct, since each participating entity type name can be used as the role name. However, in some cases the *same* entity type participates more than once in a relationship type in *different* roles. In such cases the role name becomes essential for distinguishing the meaning of the role that each participating entity plays. Such relationship types are called **recursive relationships** or **self-referencing relationships**. Figure 3.11 shows an example. The SUPERVISION relationship type relates an employee to a supervisor, where both employee and supervisor entities are members of the same EMPLOYEE entity set. Hence, the EMPLOYEE entity type *participates twice* in SUPERVISION: once in the role of *supervisor* (or *boss*), and once in the role of *supervisee* (or *subordinate*). Each relationship instance  $r_i$  in SUPERVISION associates two different employee entities  $e_j$  and  $e_k$ , one of which plays the role of supervisor and the other the role of supervisee. In Figure 3.11, the lines marked '1' represent the supervisor role, and those marked '2' represent the supervisee role; hence,  $e_1$  supervises  $e_2$  and  $e_3$ ,  $e_4$  supervises  $e_6$  and  $e_7$ , and  $e_5$  supervises  $e_1$  and  $e_4$ . In this example, each relationship instance must be connected with two lines, one marked with '1' (supervisor) and the other with '2' (supervisee).



**Figure 3.11**

A recursive relation SUPERVISION between EMPLOYEE in the *supervisor* role (1) and EMPLOYEE in the *subordinate* role (2).

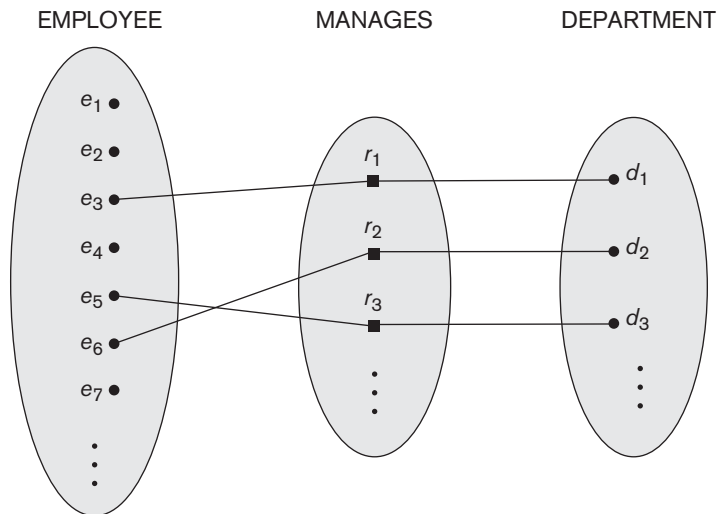
### 3.4.3 Constraints on Binary Relationship Types

Relationship types usually have certain constraints that limit the possible combinations of entities that may participate in the corresponding relationship set. These constraints are determined from the miniworld situation that the relationships represent. For example, in Figure 3.9, if the company has a rule that each employee must work for exactly one department, then we would like to describe this constraint in the schema. We can distinguish two main types of binary relationship constraints: *cardinality ratio* and *participation*.

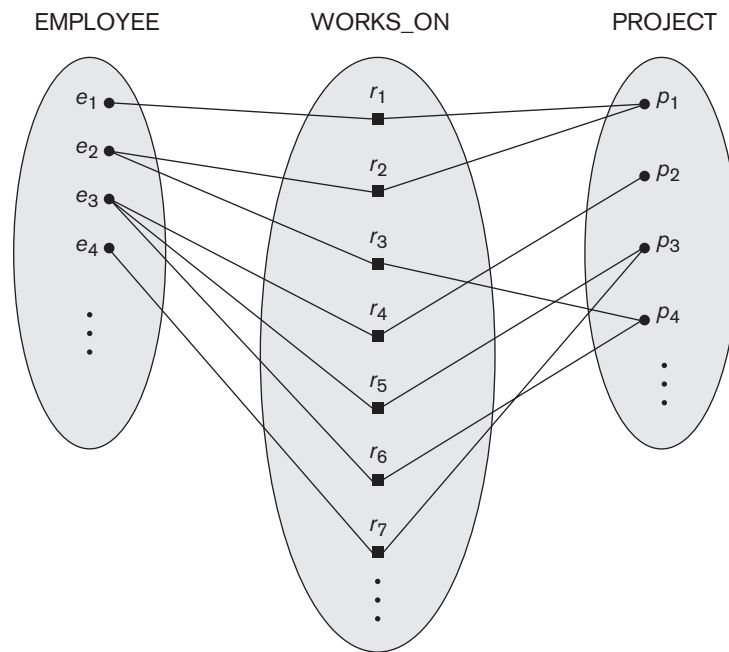
**Cardinality Ratios for Binary Relationships.** The **cardinality ratio** for a binary relationship specifies the *maximum* number of relationship instances that an entity can participate in. For example, in the WORKS\_FOR binary relationship type, DEPARTMENT:EMPLOYEE is of cardinality ratio 1:N, meaning that each department can be related to (that is, employs) any number of employees (N),<sup>9</sup> but an employee can be related to (work for) at most one department (1). This means that for this particular relationship type WORKS\_FOR, a particular department entity can be related to any number of employees (N indicates there is no maximum number). On the other hand, an employee can be related to a maximum of one department. The possible cardinality ratios for binary relationship types are 1:1, 1:N, N:1, and M:N.

An example of a 1:1 binary relationship is MANAGES (Figure 3.12), which relates a department entity to the employee who manages that department. This represents the miniworld constraints that—at any point in time—an employee can manage at

**Figure 3.12**  
A 1:1 relationship,  
MANAGES.



<sup>9</sup>N stands for *any number* of related entities (zero or more). In some notations, the asterisk symbol (\*) is used instead of N.



**Figure 3.13**  
An M:N relationship  
WORKS\_ON.

most one department and a department can have at most one manager. The relationship type WORKS\_ON (Figure 3.13) is of cardinality ratio M:N, because the miniworld rule is that an employee can work on several projects and a project can have several employees.

Cardinality ratios for binary relationships are represented on ER diagrams by displaying 1, M, and N on the diamonds as shown in Figure 3.2. Notice that in this notation, we can either specify no maximum (N) or a maximum of one (1) on participation. An alternative notation (see Section 3.7.4) allows the designer to specify a specific *maximum number* on participation, such as 4 or 5.

**Participation Constraints and Existence Dependencies.** The **participation constraint** specifies whether the existence of an entity depends on its being related to another entity via the relationship type. This constraint specifies the *minimum* number of relationship instances that each entity can participate in and is sometimes called the **minimum cardinality constraint**. There are two types of participation constraints—total and partial—that we illustrate by example. If a company policy states that *every* employee must work for a department, then an employee entity can exist only if it participates in at least one WORKS\_FOR relationship instance (Figure 3.9). Thus, the participation of EMPLOYEE in WORKS\_FOR is called **total participation**, meaning that every entity in the *total set* of employee entities must be related to a department entity via WORKS\_FOR. Total participation is also called **existence dependency**. In Figure 3.12 we do not expect every employee to manage a department, so the participation of EMPLOYEE in the

MANAGES relationship type is **partial**, meaning that *some* or *part of the set* of employee entities are related to some department entity via MANAGES, but not necessarily all. We will refer to the cardinality ratio and participation constraints, taken together, as the **structural constraints** of a relationship type.

In ER diagrams, total participation (or existence dependency) is displayed as a *double line* connecting the participating entity type to the relationship, whereas partial participation is represented by a *single line* (see Figure 3.2). Notice that in this notation, we can either specify no minimum (partial participation) or a minimum of one (total participation). An alternative notation (see Section 3.7.4) allows the designer to specify a specific *minimum number* on participation in the relationship, such as 4 or 5.

We will discuss constraints on higher-degree relationships in Section 3.9.

### 3.4.4 Attributes of Relationship Types

Relationship types can also have attributes, similar to those of entity types. For example, to record the number of hours per week that a particular employee works on a particular project, we can include an attribute Hours for the WORKS\_ON relationship type in Figure 3.13. Another example is to include the date on which a manager started managing a department via an attribute Start\_date for the MANAGES relationship type in Figure 3.12.

Notice that attributes of 1:1 or 1:N relationship types can be migrated to one of the participating entity types. For example, the Start\_date attribute for the MANAGES relationship can be an attribute of either EMPLOYEE (manager) or DEPARTMENT, although conceptually it belongs to MANAGES. This is because MANAGES is a 1:1 relationship, so every department or employee entity participates in *at most one* relationship instance. Hence, the value of the Start\_date attribute can be determined separately, either by the participating department entity or by the participating employee (manager) entity.

For a 1:N relationship type, a relationship attribute can be migrated *only* to the entity type on the N-side of the relationship. For example, in Figure 3.9, if the WORKS\_FOR relationship also has an attribute Start\_date that indicates when an employee started working for a department, this attribute can be included as an attribute of EMPLOYEE. This is because each employee works for at most one department, and hence participates in at most one relationship instance in WORKS\_FOR, but a department can have many employees, each with a different start date. In both 1:1 and 1:N relationship types, the decision where to place a relationship attribute—as a relationship type attribute or as an attribute of a participating entity type—is determined subjectively by the schema designer.

For M:N (many-to-many) relationship types, some attributes may be determined by the *combination of participating entities* in a relationship instance, not by any single entity. Such attributes *must be specified as relationship attributes*. An example is the Hours attribute of the M:N relationship WORKS\_ON (Figure 3.13); the number of hours per week an employee currently works on a project is determined by an employee-project combination and not separately by either entity.

## 3.5 Weak Entity Types

Entity types that do not have key attributes of their own are called **weak entity types**. In contrast, **regular entity types** that do have a key attribute—which include all the examples discussed so far—are called **strong entity types**. Entities belonging to a weak entity type are identified by being related to specific entities from another entity type in combination with one of their attribute values. We call this other entity type the **identifying** or **owner entity type**,<sup>10</sup> and we call the relationship type that relates a weak entity type to its owner the **identifying relationship** of the weak entity type.<sup>11</sup> A weak entity type always has a *total participation constraint* (existence dependency) with respect to its identifying relationship because a weak entity cannot be identified without an owner entity. However, not every existence dependency results in a weak entity type. For example, a DRIVER\_LICENSE entity cannot exist unless it is related to a PERSON entity, even though it has its own key (License\_number) and hence is not a weak entity.

Consider the entity type DEPENDENT, related to EMPLOYEE, which is used to keep track of the dependents of each employee via a 1:N relationship (Figure 3.2). In our example, the attributes of DEPENDENT are Name (the first name of the dependent), Birth\_date, Sex, and Relationship (to the employee). Two dependents of *two distinct employees* may, by chance, have the same values for Name, Birth\_date, Sex, and Relationship, but they are still distinct entities. They are identified as distinct entities only after determining the *particular employee entity* to which each dependent is related. Each employee entity is said to *own* the dependent entities that are related to it.

A weak entity type normally has a **partial key**, which is the attribute that can uniquely identify weak entities that are *related to the same owner entity*.<sup>12</sup> In our example, if we assume that no two dependents of the same employee ever have the same first name, the attribute Name of DEPENDENT is the partial key. In the worst case, a composite attribute of *all the weak entity's attributes* will be the partial key.

In ER diagrams, both a weak entity type and its identifying relationship are distinguished by surrounding their boxes and diamonds with double lines (see Figure 3.2). The partial key attribute is underlined with a dashed or dotted line.

Weak entity types can sometimes be represented as complex (composite, multivalued) attributes. In the preceding example, we could specify a multivalued attribute Dependents for EMPLOYEE, which is a multivalued composite attribute with the component attributes Name, Birth\_date, Sex, and Relationship. The choice of which representation to use is made by the database designer. One criterion that may be used is to choose the weak entity type representation if the weak entity type participates independently in relationship types other than its identifying relationship type.

In general, any number of levels of weak entity types can be defined; an owner entity type may itself be a weak entity type. In addition, a weak entity type may have more than one identifying entity type and an identifying relationship type of degree higher than two, as we illustrate in Section 3.9.

---

<sup>10</sup>The identifying entity type is also sometimes called the **parent entity type** or the **dominant entity type**.

<sup>11</sup>The weak entity type is also sometimes called the **child entity type** or the **subordinate entity type**.

<sup>12</sup>The partial key is sometimes called the **discriminator**.

## 3.6 Refining the ER Design for the COMPANY Database

We can now refine the database design in Figure 3.8 by changing the attributes that represent relationships into relationship types. The cardinality ratio and participation constraint of each relationship type are determined from the requirements listed in Section 3.2. If some cardinality ratio or dependency cannot be determined from the requirements, the users must be questioned further to determine these structural constraints.

In our example, we specify the following relationship types:

- MANAGES, which is a 1:1(one-to-one) relationship type between EMPLOYEE and DEPARTMENT. EMPLOYEE participation is partial. DEPARTMENT participation is not clear from the requirements. We question the users, who say that a department must have a manager at all times, which implies total participation.<sup>13</sup> The attribute Start\_date is assigned to this relationship type.
- WORKS\_FOR, a 1:N (one-to-many) relationship type between DEPARTMENT and EMPLOYEE. Both participations are total.
- CONTROLS, a 1:N relationship type between DEPARTMENT and PROJECT. The participation of PROJECT is total, whereas that of DEPARTMENT is determined to be partial, after consultation with the users indicates that some departments may control no projects.
- SUPERVISION, a 1:N relationship type between EMPLOYEE (in the supervisor role) and EMPLOYEE (in the supervisee role). Both participations are determined to be partial, after the users indicate that not every employee is a supervisor and not every employee has a supervisor.
- WORKS\_ON, determined to be an M:N (many-to-many) relationship type with attribute Hours, after the users indicate that a project can have several employees working on it. Both participations are determined to be total.
- DEPENDENTS\_OF, a 1:N relationship type between EMPLOYEE and DEPENDENT, which is also the identifying relationship for the weak entity type DEPENDENT. The participation of EMPLOYEE is partial, whereas that of DEPENDENT is total.

After specifying the previous six relationship types, we remove from the entity types in Figure 3.8 all attributes that have been refined into relationships. These include Manager and Manager\_start\_date from DEPARTMENT; Controlling\_department from PROJECT; Department, Supervisor, and Works\_on from EMPLOYEE; and Employee from DEPENDENT. It is important to have the least possible redundancy when we design the conceptual schema of a database. If some redundancy is desired at the storage level or at the user view level, it can be introduced later, as discussed in Section 1.6.1.

---

<sup>13</sup>The rules in the miniworld that determine the constraints are sometimes called the *business rules*, since they are determined by the *business* or organization that will utilize the database.

## 3.7 ER Diagrams, Naming Conventions, and Design Issues

### 3.7.1 Summary of Notation for ER Diagrams

Figures 3.9 through 3.13 illustrate examples of the participation of entity types in relationship types by displaying their entity sets and relationship sets (or extensions)—the individual entity instances in an entity set and the individual relationship instances in a relationship set. In ER diagrams the emphasis is on representing the schemas rather than the instances. This is more useful in database design because a database schema changes rarely, whereas the contents of the entity sets may change frequently. In addition, the schema is obviously easier to display, because it is much smaller.

Figure 3.2 displays the COMPANY ER database schema as an ER diagram. We now review the full ER diagram notation. Regular (strong) entity types such as EMPLOYEE, DEPARTMENT, and PROJECT are shown in rectangular boxes. Relationship types such as WORKS\_FOR, MANAGES, CONTROLS, and WORKS\_ON are shown in diamond-shaped boxes attached to the participating entity types with straight lines. Attributes are shown in ovals, and each attribute is attached by a straight line to its entity type or relationship type. Component attributes of a composite attribute are attached to the oval representing the composite attribute, as illustrated by the Name attribute of EMPLOYEE. Multivalued attributes are shown in double ovals, as illustrated by the Locations attribute of DEPARTMENT. Key attributes have their names underlined. Derived attributes are shown in dotted ovals, as illustrated by the Number\_of\_employees attribute of DEPARTMENT.

Weak entity types are distinguished by being placed in double rectangles and by having their identifying relationship placed in double diamonds, as illustrated by the DEPENDENT entity type and the DEPENDENTS\_OF identifying relationship type. The partial key of the weak entity type is underlined with a dotted line.

In Figure 3.2 the cardinality ratio of each *binary* relationship type is specified by attaching a 1, M, or N on each participating edge. The cardinality ratio of DEPARTMENT:EMPLOYEE in MANAGES is 1:1, whereas it is 1:N for DEPARTMENT:EMPLOYEE in WORKS\_FOR, and M:N for WORKS\_ON. The participation constraint is specified by a single line for partial participation and by double lines for total participation (existence dependency).

In Figure 3.2 we show the role names for the SUPERVISION relationship type because the same EMPLOYEE entity type plays two distinct roles in that relationship. Notice that the cardinality ratio is 1:N from supervisor to supervisee because each employee in the role of supervisee has at most one direct supervisor, whereas an employee in the role of supervisor can supervise zero or more employees.

Figure 3.14 summarizes the conventions for ER diagrams. It is important to note that there are many other alternative diagrammatic notations (see Section 3.7.4 and Appendix A).

### 3.7.2 Proper Naming of Schema Constructs

When designing a database schema, the choice of names for entity types, attributes, relationship types, and (particularly) roles is not always straightforward. One should choose names that convey, as much as possible, the meanings attached to the different constructs in the schema. We choose to use *singular names* for entity types, rather than plural ones, because the entity type name applies to each individual entity belonging to that entity type. In our ER diagrams, we will use the convention that entity type and relationship type names are in uppercase letters, attribute names have their initial letter capitalized, and role names are in lowercase letters. We have used this convention in Figure 3.2.

As a general practice, given a narrative description of the database requirements, the *nouns* appearing in the narrative tend to give rise to entity type names, and the *verbs* tend to indicate names of relationship types. Attribute names generally arise from additional nouns that describe the nouns corresponding to entity types.

Another naming consideration involves choosing binary relationship names to make the ER diagram of the schema readable from left to right and from top to bottom. We have generally followed this guideline in Figure 3.2. To explain this naming convention further, we have one exception to the convention in Figure 3.2—the `DEPENDENTS_OF` relationship type, which reads from bottom to top. When we describe this relationship, we can say that the `DEPENDENT` entities (bottom entity type) are `DEPENDENTS_OF` (relationship name) an `EMPLOYEE` (top entity type). To change this to read from top to bottom, we could rename the relationship type to `HAS_DEPENDENTS`, which would then read as follows: An `EMPLOYEE` entity (top entity type) `HAS_DEPENDENTS` (relationship name) of type `DEPENDENT` (bottom entity type). Notice that this issue arises because each binary relationship can be described starting from either of the two participating entity types, as discussed in the beginning of Section 3.4.

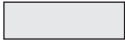
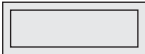





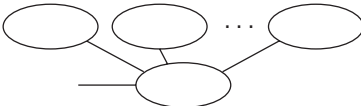

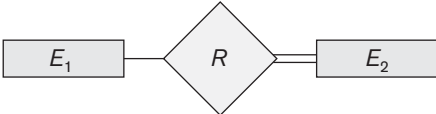
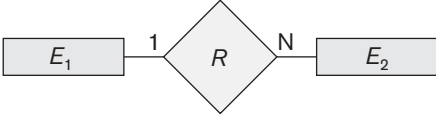
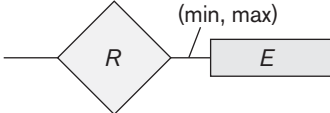
### 3.7.3 Design Choices for ER Conceptual Design

It is occasionally difficult to decide whether a particular concept in the miniworld should be modeled as an entity type, an attribute, or a relationship type. In this section, we give some brief guidelines as to which construct should be chosen in particular situations.

In general, the schema design process should be considered an iterative refinement process, where an initial design is created and then iteratively refined until the most suitable design is reached. Some of the refinements that are often used include the following:

- A concept may be first modeled as an attribute and then refined into a relationship because it is determined that the attribute is a reference to another entity type. It is often the case that a pair of such attributes that are inverses of one another are refined into a binary relationship. We discussed this type of refinement in detail in Section 3.6. It is important to note that in our notation,



Symbol	Meaning
	Entity
	Weak Entity
	Relationship
	Identifying Relationship
	Attribute
	Key Attribute
	Multivalued Attribute
	Composite Attribute
	Derived Attribute
	Total Participation of $E_2$ in $R$
	Cardinality Ratio 1 : N for $E_1 : E_2$ in $R$
	Structural Constraint (min, max) on Participation of $E$ in $R$

**Figure 3.14**  
Summary of the notation for ER diagrams.

once an attribute is replaced by a relationship, the attribute itself should be removed from the entity type to avoid duplication and redundancy.

- Similarly, an attribute that exists in several entity types may be elevated or promoted to an independent entity type. For example, suppose that each of several entity types in a UNIVERSITY database, such as STUDENT, INSTRUCTOR, and COURSE, has an attribute Department in the initial design; the designer may then choose to create an entity type DEPARTMENT with a single attribute Dept\_name and relate it to the three entity types (STUDENT, INSTRUCTOR, and COURSE) via appropriate relationships. Other attributes/relationships of DEPARTMENT may be discovered later.
- An inverse refinement to the previous case may be applied—for example, if an entity type DEPARTMENT exists in the initial design with a single attribute Dept\_name and is related to only one other entity type, STUDENT. In this case, DEPARTMENT may be reduced or demoted to an attribute of STUDENT.
- Section 3.9 discusses choices concerning the degree of a relationship. In Chapter 4, we discuss other refinements concerning specialization/generalization.

### 3.7.4 Alternative Notations for ER Diagrams

There are many alternative diagrammatic notations for displaying ER diagrams. Appendix A gives some of the more popular notations. In Section 3.8, we introduce the Unified Modeling Language (UML) notation for class diagrams, which has been proposed as a standard for conceptual object modeling.

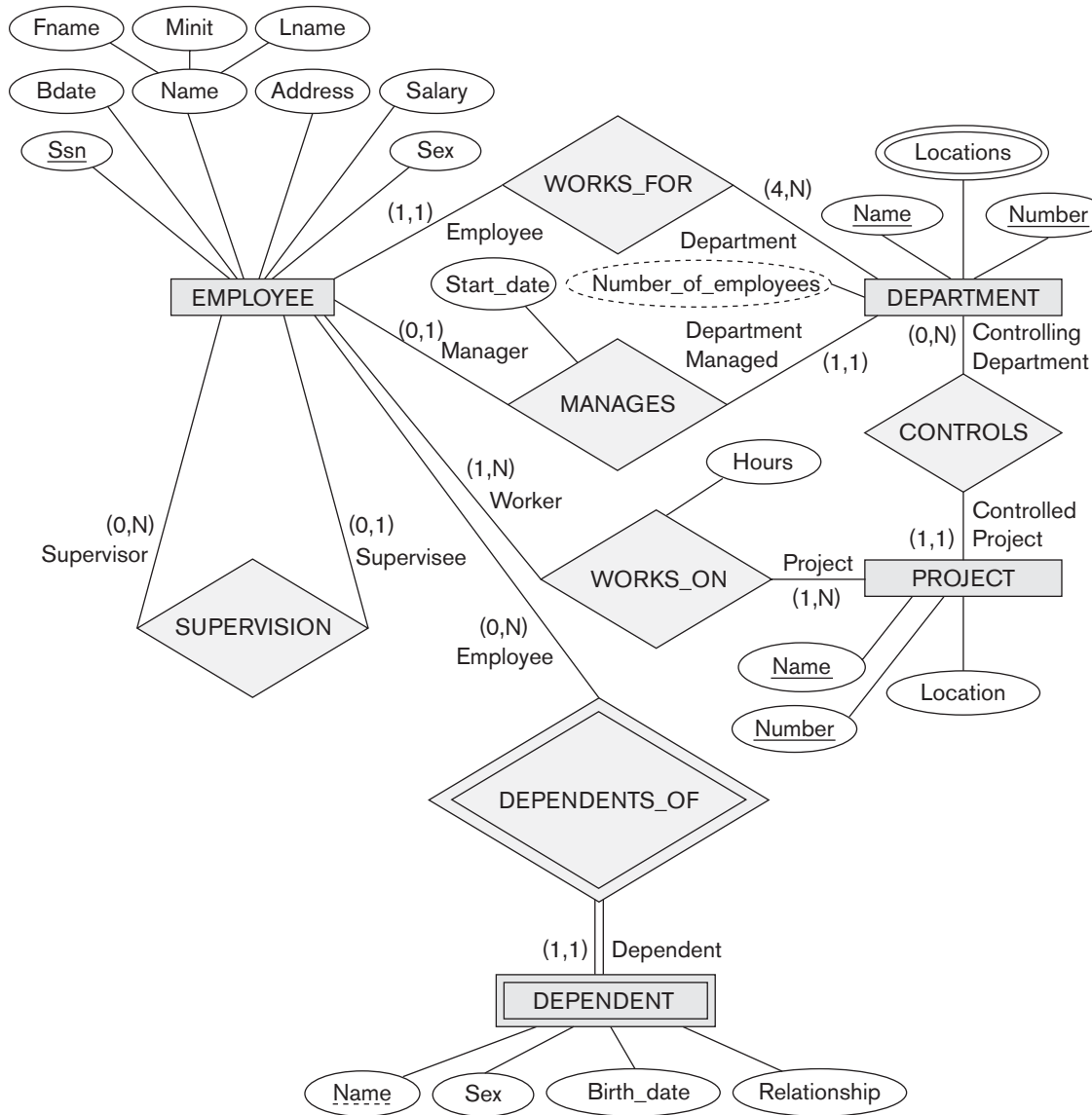
In this section, we describe one alternative ER notation for specifying structural constraints on relationships, which replaces the cardinality ratio (1:1, 1:N, M:N) and single/double-line notation for participation constraints. This notation involves associating a pair of integer numbers (min, max) with each *participation* of an entity type  $E$  in a relationship type  $R$ , where  $0 \leq \min \leq \max$  and  $\max \geq 1$ . The numbers mean that for each entity  $e$  in  $E$ ,  $e$  must participate in at least  $\min$  and at most  $\max$  relationship instances in  $R$  at any point in time. In this method,  $\min = 0$  implies partial participation, whereas  $\min > 0$  implies total participation.

Figure 3.15 displays the COMPANY database schema using the (min, max) notation.<sup>14</sup> Usually, one uses either the cardinality ratio/single-line/double-line notation *or* the (min, max) notation. The (min, max) notation is more precise, and we can use it to specify some structural constraints for relationship types of *higher degree*. However, it is not sufficient for specifying some key constraints on higher-degree relationships, as discussed in Section 3.9.

Figure 3.15 also displays all the role names for the COMPANY database schema.

---

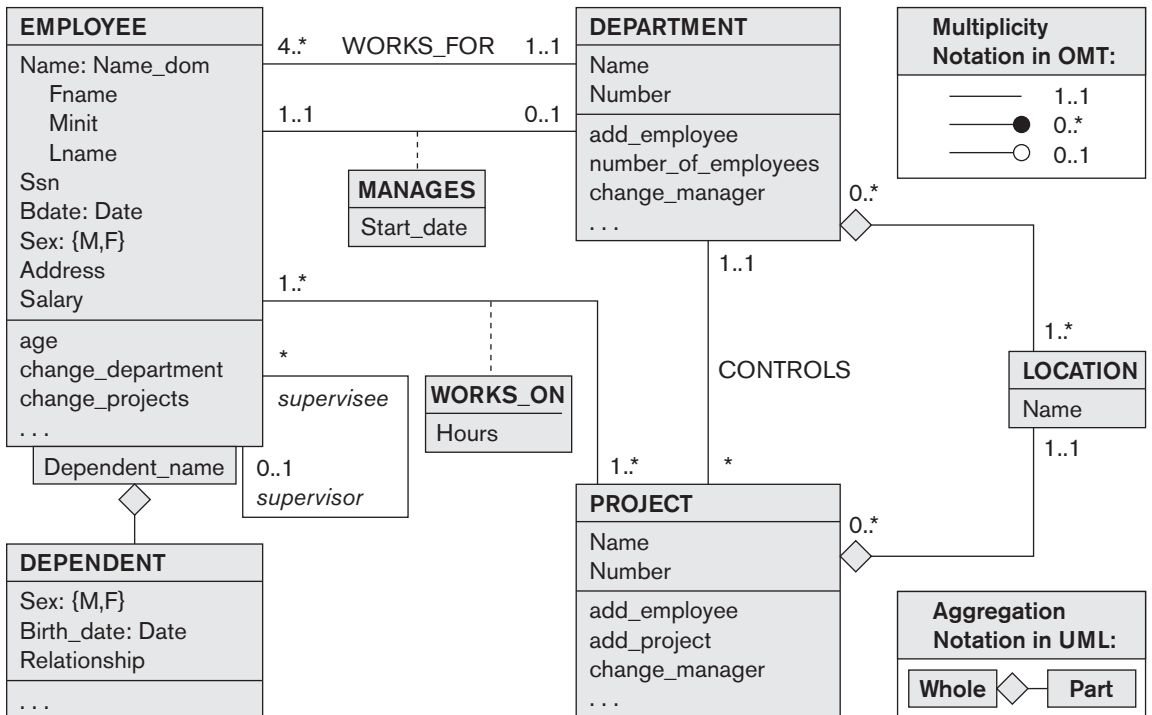
<sup>14</sup>In some notations, particularly those used in object modeling methodologies such as UML, the (min, max) is placed on the *opposite sides* to the ones we have shown. For example, for the WORKS\_FOR relationship in Figure 3.15, the (1,1) would be on the DEPARTMENT side, and the (4,N) would be on the EMPLOYEE side. Here we used the original notation from Abrial (1974).



**Figure 3.15**  
ER diagrams for the company schema, with structural constraints specified using (min, max) notation and role names.

### 3.8 Example of Other Notation: UML Class Diagrams

The UML methodology is being used extensively in software design and has many types of diagrams for various software design purposes. We only briefly present the basics of UML class diagrams here and compare them with ER diagrams. In some



**Figure 3.16**

The COMPANY conceptual schema in UML class diagram notation.

ways, class diagrams can be considered as an alternative notation to ER diagrams. Additional UML notation and concepts are presented in Section 8.6. Figure 3.16 shows how the COMPANY ER database schema in Figure 3.15 can be displayed using UML class diagram notation. The *entity types* in Figure 3.15 are modeled as *classes* in Figure 3.16. An *entity* in ER corresponds to an *object* in UML.

In UML class diagrams, a **class** (similar to an entity type in ER) is displayed as a box (see Figure 3.16) that includes three sections: The top section gives the **class name** (similar to entity type name); the middle section includes the **attributes**; and the last section includes **operations** that can be applied to individual objects (similar to individual entities in an entity set) of the class. Operations are *not* specified in ER diagrams. Consider the EMPLOYEE class in Figure 3.16. Its attributes are Name, Ssn, Bdate, Sex, Address, and Salary. The designer can optionally specify the **domain** (or data type) of an attribute if desired, by placing a colon (:) followed by the domain name or description, as illustrated by the Name, Sex, and Bdate attributes of EMPLOYEE in Figure 3.16. A composite attribute is modeled as a **structured domain**, as illustrated by the Name attribute of EMPLOYEE. A multivalued attribute will generally be modeled as a separate class, as illustrated by the LOCATION class in Figure 3.16.

Relationship types are called **associations** in UML terminology, and relationship instances are called **links**. A **binary association** (binary relationship type) is represented as a line connecting the participating classes (entity types), and may optionally have a name. A relationship attribute, called a **link attribute**, is placed in a box that is connected to the association's line by a dashed line. The (min, max) notation described in Section 3.7.4 is used to specify relationship constraints, which are called **multiplicities** in UML terminology. Multiplicities are specified in the form *min..max*, and an asterisk (\*) indicates no maximum limit on participation. However, the multiplicities are placed *on the opposite ends of the relationship* when compared with the (min, max) notation discussed in Section 3.7.4 (compare Figures 3.15 and 3.16). In UML, a single asterisk indicates a multiplicity of 0..\*, and a single 1 indicates a multiplicity of 1..1. A recursive relationship type (see Section 3.4.2) is called a **reflexive association** in UML, and the role names—like the multiplicities—are placed at the opposite ends of an association when compared with the placing of role names in Figure 3.15.

In UML, there are two types of relationships: association and aggregation. **Aggregation** is meant to represent a relationship between a whole object and its component parts, and it has a distinct diagrammatic notation. In Figure 3.16, we modeled the locations of a department and the single location of a project as aggregations. However, aggregation and association do not have different structural properties, and the choice as to which type of relationship to use—aggregation or association—is somewhat subjective. In the ER model, both are represented as relationships.

UML also distinguishes between **unidirectional** and **bidirectional** associations (or aggregations). In the unidirectional case, the line connecting the classes is displayed with an arrow to indicate that only one direction for accessing related objects is needed. If no arrow is displayed, the bidirectional case is assumed, which is the default. For example, if we always expect to access the manager of a department starting from a DEPARTMENT object, we would draw the association line representing the MANAGES association with an arrow from DEPARTMENT to EMPLOYEE. In addition, relationship instances may be specified to be **ordered**. For example, we could specify that the employee objects related to each department through the WORKS\_FOR association (relationship) should be ordered by their Start\_date attribute value. Association (relationship) names are *optional* in UML, and relationship attributes are displayed in a box attached with a dashed line to the line representing the association/aggregation (see Start\_date and Hours in Figure 3.16).

The operations given in each class are derived from the functional requirements of the application, as we discussed in Section 3.1. It is generally sufficient to specify the operation names initially for the logical operations that are expected to be applied to individual objects of a class, as shown in Figure 3.16. As the design is refined, more details are added, such as the exact argument types (parameters) for each operation, plus a functional description of each operation. UML has *function descriptions* and *sequence diagrams* to specify some of the operation details, but these are beyond the scope of our discussion.

Weak entities can be modeled using the UML construct called **qualified association** (or **qualified aggregation**); this can represent both the identifying relationship and the partial key, which is placed in a box attached to the owner class. This is illustrated by the `DEPENDENT` class and its qualified aggregation to `EMPLOYEE` in Figure 3.16. In UML terminology, the partial key attribute `Dependent_name` is called the **discriminator**, because its value distinguishes the objects associated with (related to) the same `EMPLOYEE` entity. Qualified associations are not restricted to modeling weak entities, and they can be used to model other situations in UML.

This section is not meant to be a complete description of UML class diagrams, but rather to illustrate one popular type of alternative diagrammatic notation that can be used for representing ER modeling concepts.

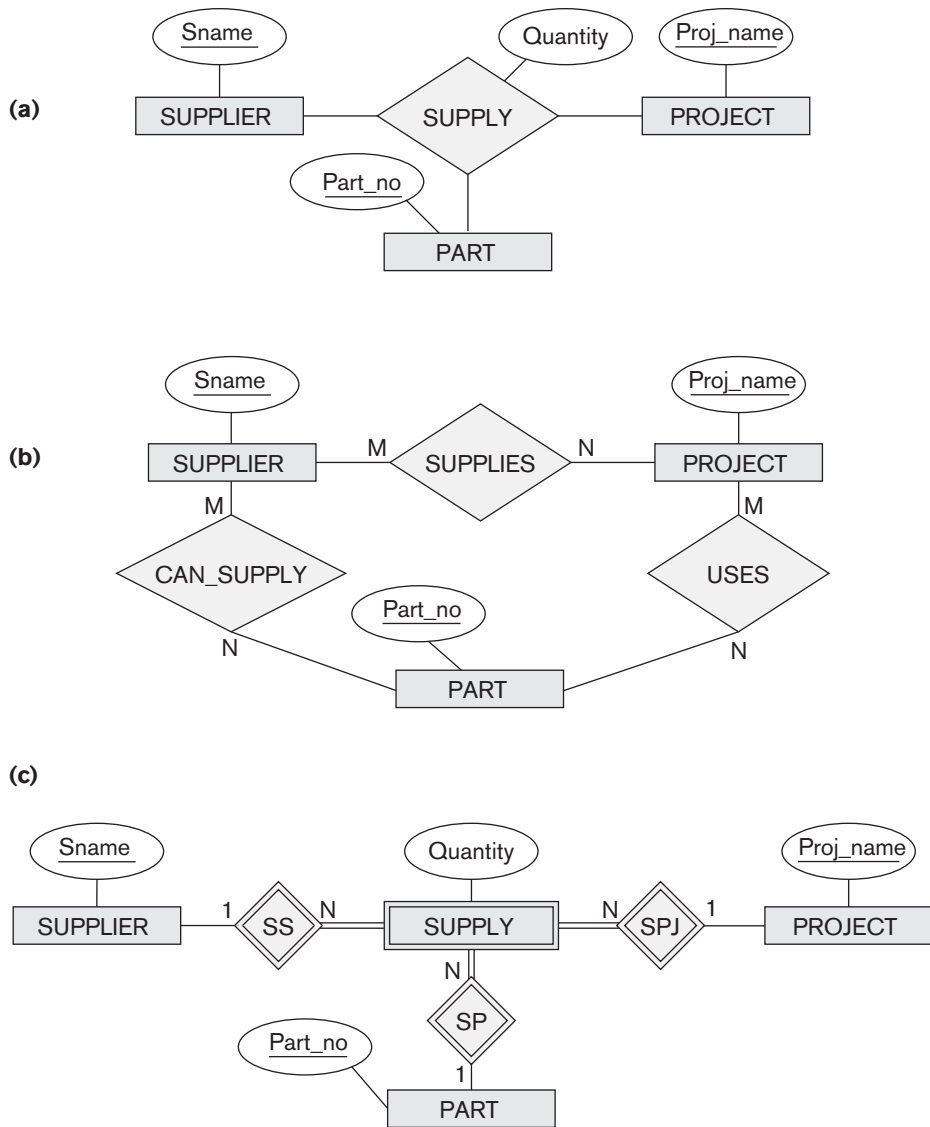
## 3.9 Relationship Types of Degree Higher than Two

In Section 3.4.2 we defined the **degree** of a relationship type as the number of participating entity types and called a relationship type of degree two *binary* and a relationship type of degree three *ternary*. In this section, we elaborate on the differences between binary and higher-degree relationships, when to choose higher-degree versus binary relationships, and how to specify constraints on higher-degree relationships.

### 3.9.1 Choosing between Binary and Ternary (or Higher-Degree) Relationships

The ER diagram notation for a ternary relationship type is shown in Figure 3.17(a), which displays the schema for the `SUPPLY` relationship type that was displayed at the instance level in Figure 3.10. Recall that the relationship set of `SUPPLY` is a set of relationship instances  $(s, j, p)$ , where the meaning is that  $s$  is a `SUPPLIER` who is currently supplying a `PART`  $p$  to a `PROJECT`  $j$ . In general, a relationship type  $R$  of degree  $n$  will have  $n$  edges in an ER diagram, one connecting  $R$  to each participating entity type.

Figure 3.17(b) shows an ER diagram for three binary relationship types `CAN_SUPPLY`, `USES`, and `SUPPLIES`. In general, a ternary relationship type represents different information than do three binary relationship types. Consider the three binary relationship types `CAN_SUPPLY`, `USES`, and `SUPPLIES`. Suppose that `CAN_SUPPLY`, between `SUPPLIER` and `PART`, includes an instance  $(s, p)$  whenever supplier  $s$  can supply part  $p$  (to any project); `USES`, between `PROJECT` and `PART`, includes an instance  $(j, p)$  whenever project  $j$  uses part  $p$ ; and `SUPPLIES`, between `SUPPLIER` and `PROJECT`, includes an instance  $(s, j)$  whenever supplier  $s$  supplies some part to project  $j$ . The existence of three relationship instances  $(s, p)$ ,  $(j, p)$ , and  $(s, j)$  in `CAN_SUPPLY`, `USES`, and `SUPPLIES`, respectively, does not necessarily imply that an instance  $(s, j, p)$  exists in the ternary relationship `SUPPLY`, because the *meaning is different*. It is often tricky to decide whether a particular relationship should be represented as a relationship type of degree  $n$  or should be



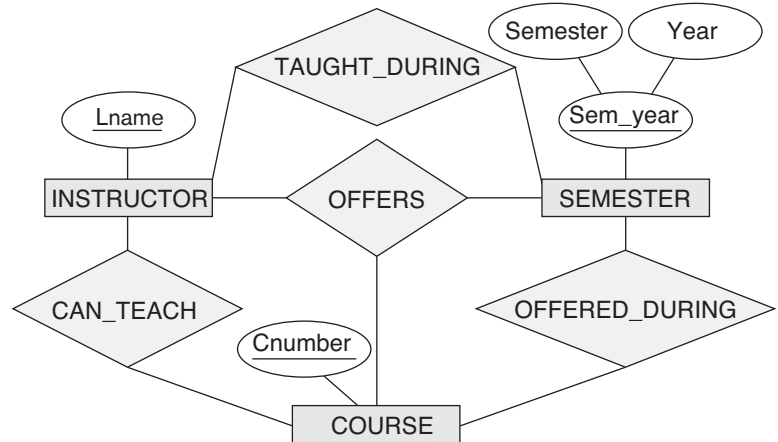
**Figure 3.17**

Ternary relationship types. (a) The SUPPLY relationship. (b) Three binary relationships not equivalent to SUPPLY. (c) SUPPLY represented as a weak entity type.

broken down into several relationship types of smaller degrees. The designer must base this decision on the semantics or meaning of the particular situation being represented. The typical solution is to include the ternary relationship *plus* one or more of the binary relationships, if they represent different meanings and if all are needed by the application.

**Figure 3.18**

Another example of ternary versus binary relationship types.

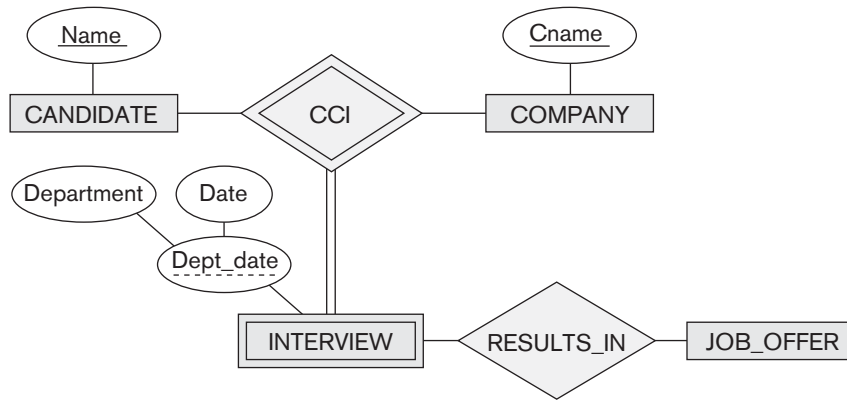


Some database design tools are based on variations of the ER model that permit only binary relationships. In this case, a ternary relationship such as SUPPLY must be represented as a weak entity type, with no partial key and with three identifying relationships. The three participating entity types SUPPLIER, PART, and PROJECT are together the owner entity types (see Figure 3.17(c)). Hence, an entity in the weak entity type SUPPLY in Figure 3.17(c) is identified by the combination of its three owner entities from SUPPLIER, PART, and PROJECT.

It is also possible to represent the ternary relationship as a regular entity type by introducing an artificial or surrogate key. In this example, a key attribute Supply\_id could be used for the supply entity type, converting it into a regular entity type. Three binary N:1 relationships relate SUPPLY to each of the three participating entity types.

Another example is shown in Figure 3.18. The ternary relationship type OFFERS represents information on instructors offering courses during particular semesters; hence it includes a relationship instance  $(i, s, c)$  whenever INSTRUCTOR  $i$  offers COURSE  $c$  during SEMESTER  $s$ . The three binary relationship types shown in Figure 3.18 have the following meanings: CAN\_TEACH relates a course to the instructors who *can teach* that course, TAUGHT\_DURING relates a semester to the instructors who *taught some course* during that semester, and OFFERED\_DURING relates a semester to the courses offered during that semester *by any instructor*. These ternary and binary relationships represent different information, but certain constraints should hold among the relationships. For example, a relationship instance  $(i, s, c)$  should not exist in OFFERS *unless* an instance  $(i, s)$  exists in TAUGHT\_DURING, an instance  $(s, c)$  exists in OFFERED\_DURING, and an instance  $(i, c)$  exists in CAN\_TEACH. However, the reverse is not always true; we may have instances  $(i, s)$ ,  $(s, c)$ , and  $(i, c)$  in the three binary relationship types with no corresponding instance  $(i, s, c)$  in OFFERS. Note that in this example, based on the meanings of the relationships, we can infer the instances of TAUGHT\_DURING and OFFERED\_DURING from the instances in OFFERS, but





**Figure 3.19**  
A weak entity type INTERVIEW with a ternary identifying relationship type.

we cannot infer the instances of CAN\_TEACH; therefore, TAUGHT\_DURING and OFFERED\_DURING are redundant and can be left out.

Although in general three binary relationships *cannot* replace a ternary relationship, they may do so under certain *additional constraints*. In our example, if the CAN\_TEACH relationship is 1:1 (an instructor can teach only one course, and a course can be taught by only one instructor), then the ternary relationship OFFERS can be left out because it can be inferred from the three binary relationships CAN\_TEACH, TAUGHT\_DURING, and OFFERED\_DURING. The schema designer must analyze the meaning of each specific situation to decide which of the binary and ternary relationship types are needed.

Notice that it is possible to have a weak entity type with a ternary (or  $n$ -ary) identifying relationship type. In this case, the weak entity type can have *several* owner entity types. An example is shown in Figure 3.19. This example shows part of a database that keeps track of candidates interviewing for jobs at various companies, which may be part of an employment agency database. In the requirements, a candidate can have multiple interviews with the same company (for example, with different company departments or on separate dates), but a job offer is made based on one of the interviews. Here, INTERVIEW is represented as a weak entity with two owners CANDIDATE and COMPANY, and with the partial key Dept\_date. An INTERVIEW entity is uniquely identified by a candidate, a company, and the combination of the date and department of the interview.

### 3.9.2 Constraints on Ternary (or Higher-Degree) Relationships

There are two notations for specifying structural constraints on  $n$ -ary relationships, and they specify different constraints. They should thus *both be used* if it is important to fully specify the structural constraints on a ternary or higher-degree relationship. The first notation is based on the cardinality ratio notation of binary relationships displayed in Figure 3.2. Here, a 1, M, or N is specified on each

participation arc (both M and N symbols stand for *many* or *any number*).<sup>15</sup> Let us illustrate this constraint using the SUPPLY relationship in Figure 3.17.

Recall that the relationship set of SUPPLY is a set of relationship instances  $(s, j, p)$ , where  $s$  is a SUPPLIER,  $j$  is a PROJECT, and  $p$  is a PART. Suppose that the constraint exists that for a particular project-part combination, only one supplier will be used (only one supplier supplies a particular part to a particular project). In this case, we place 1 on the SUPPLIER participation, and M, N on the PROJECT, PART participations in Figure 3.17. This specifies the constraint that a particular  $(j, p)$  combination can appear at most once in the relationship set because each such (PROJECT, PART) combination uniquely determines a single supplier. Hence, any relationship instance  $(s, j, p)$  is uniquely identified in the relationship set by its  $(j, p)$  combination, which makes  $(j, p)$  a key for the relationship set. In this notation, the participations that have a 1 specified on them are not required to be part of the identifying key for the relationship set.<sup>16</sup> If all three cardinalities are M or N, then the key will be the combination of all three participants.

The second notation is based on the (min, max) notation displayed in Figure 3.15 for binary relationships. A (min, max) on a participation here specifies that each entity is related to at least *min* and at most *max relationship instances* in the relationship set. These constraints have no bearing on determining the key of an  $n$ -ary relationship, where  $n > 2$ ,<sup>17</sup> but specify a different type of constraint that places restrictions on how many relationship instances each entity can participate in.

### 3.10 Another Example: A UNIVERSITY Database

We now present another example, a UNIVERSITY database, to illustrate the ER modeling concepts. Suppose that a database is needed to keep track of student enrollments in classes and students' final grades. After analyzing the miniworld rules and the users' needs, the requirements for this database were determined to be as follows (for brevity, we show the chosen entity type names and attribute names for the conceptual schema in parentheses as we describe the requirements; relationship type names are only shown in the ER schema diagram):

- The university is organized into colleges (COLLEGE), and each college has a unique name (CName), a main office (COffice) and phone (CPhone), and a particular faculty member who is dean of the college. Each college administers a number of academic departments (DEPT). Each department has a unique name (DName), a unique code number (DCode), a main office (DOffice) and phone (DPhone), and a particular faculty member who chairs the department. We keep track of the start date (CStartDate) when that faculty member began chairing the department.

---

<sup>15</sup>This notation allows us to determine the key of the *relationship relation*, as we discuss in Chapter 9.

<sup>16</sup>This is also true for cardinality ratios of binary relationships.

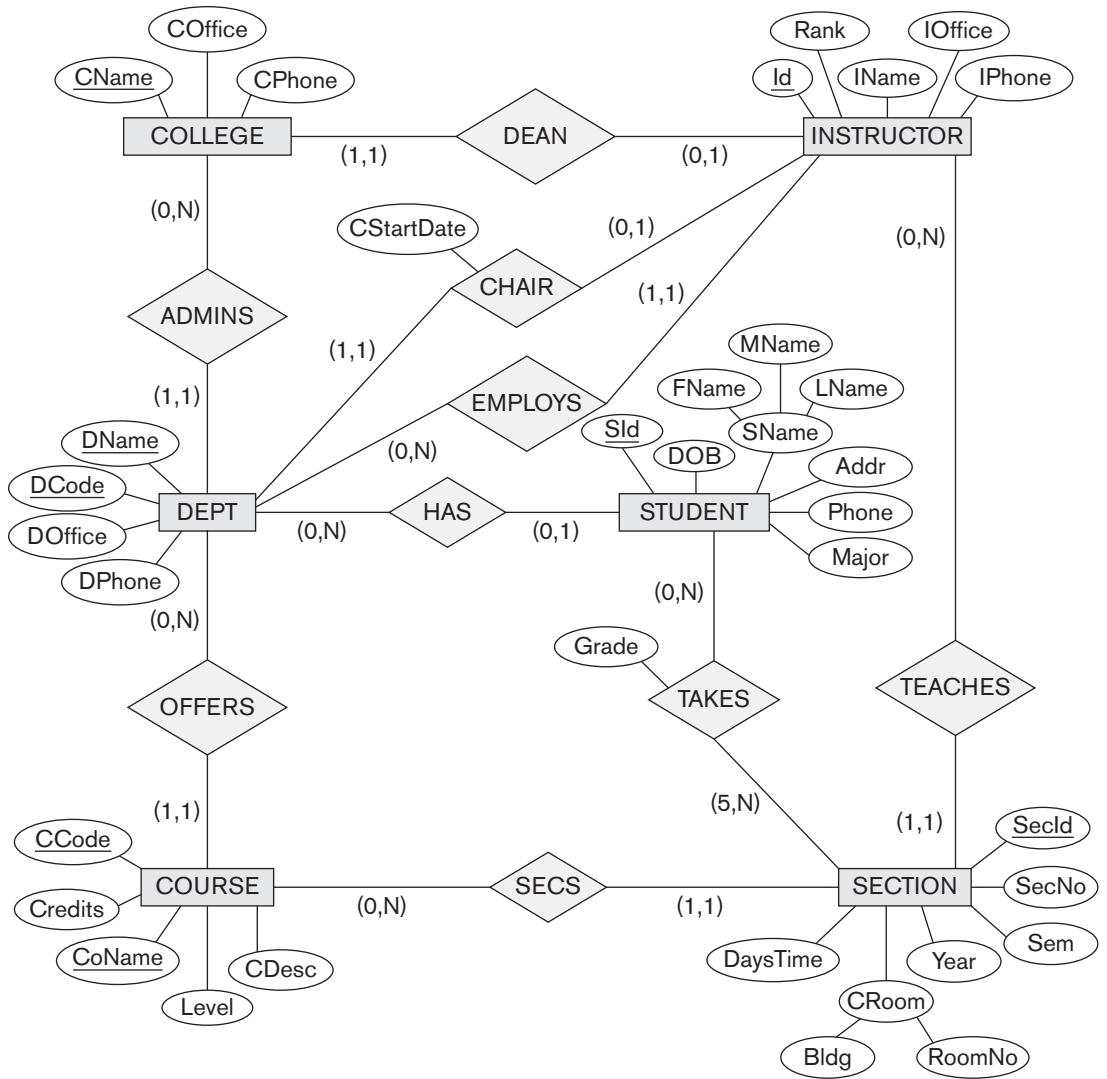
<sup>17</sup>The (min, max) constraints can determine the keys for binary relationships.

- A department offers a number of courses (COURSE), each of which has a unique course name (CoName), a unique code number (CCode), a course level (Level: this can be coded as 1 for freshman level, 2 for sophomore, 3 for junior, 4 for senior, 5 for MS level, and 6 for PhD level), a course credit hours (Credits), and a course description (CDesc). The database also keeps track of instructors (INSTRUCTOR); and each instructor has a unique identifier (Id), name (IName), office (IOffice), phone (IPhone), and rank (Rank); in addition, each instructor works for one primary academic department.
- The database will keep student data (STUDENT) and stores each student's name (SName, composed of first name (FName), middle name (MName), last name (LName)), student id (Sid, unique for every student), address (Addr), phone (Phone), major code (Major), and date of birth (DoB). A student is assigned to one primary academic department. It is required to keep track of the student's grades in each section the student has completed.
- Courses are offered as sections (SECTION). Each section is related to a single course and a single instructor and has a unique section identifier (SecId). A section also has a section number (SecNo: this is coded as 1, 2, 3, . . . for multiple sections offered during the same semester/year), semester (Sem), year (Year), classroom (CRoom: this is coded as a combination of building code (Bldg) and room number (RoomNo) within the building), and days/times (DaysTime: for example, 'MWF 9am-9.50am' or 'TR 3.30pm-5.20pm'—restricted to only allowed days/time values). (*Note:* The database will keep track of all the sections offered for the past several years, in addition to the current offerings. The SecId is unique for all sections, not just the sections for a particular semester.) The database keeps track of the students in each section, and the grade is recorded when available (this is a many-to-many relationship between students and sections). A section must have at least five students.

The ER diagram for these requirements is shown in Figure 3.20 using the min-max ER diagrammatic notation. Notice that for the SECTION entity type, we only showed SecID as an underlined key, but because of the miniworld constraints, several other combinations of values have to be unique for each section entity. For example, each of the following combinations must be unique based on the typical miniworld constraints:

1. (SecNo, Sem, Year, CCode (of the COURSE related to the SECTION)): This specifies that the section numbers of a particular course must be different during each particular semester and year.
2. (Sem, Year, CRoom, DaysTime): This specifies that in a particular semester and year, a classroom cannot be used by two different sections at the same days/time.
3. (Sem, Year, DaysTime, Id (of the INSTRUCTOR teaching the SECTION)): This specifies that in a particular semester and year, an instructor cannot teach two sections at the same days/time. Note that this rule will not apply if an instructor is allowed to teach two combined sections together in the particular university.

Can you think of any other attribute combinations that have to be unique?



**Figure 3.20**  
An ER diagram for a UNIVERSITY database schema.

### 3.11 Summary

In this chapter we presented the modeling concepts of a high-level conceptual data model, the entity-relationship (ER) model. We started by discussing the role that a high-level data model plays in the database design process, and then we presented a sample set of database requirements for the COMPANY database, which is one of the

examples that is used throughout this text. We defined the basic ER model concepts of entities and their attributes. Then we discussed NULL values and presented the various types of attributes, which can be nested arbitrarily to produce complex attributes:

- Simple or atomic
- Composite
- Multivalued

We also briefly discussed stored versus derived attributes. Then we discussed the ER model concepts at the schema or “intension” level:

- Entity types and their corresponding entity sets
- Key attributes of entity types
- Value sets (domains) of attributes
- Relationship types and their corresponding relationship sets
- Participation roles of entity types in relationship types

We presented two methods for specifying the structural constraints on relationship types. The first method distinguished two types of structural constraints:

- Cardinality ratios (1:1, 1:N, M:N for binary relationships)
- Participation constraints (total, partial)

We noted that, alternatively, another method of specifying structural constraints is to specify minimum and maximum numbers (min, max) on the participation of each entity type in a relationship type. We discussed weak entity types and the related concepts of owner entity types, identifying relationship types and partial key attributes.

Entity–relationship schemas can be represented diagrammatically as ER diagrams. We showed how to design an ER schema for the COMPANY database by first defining the entity types and their attributes and then refining the design to include relationship types. We displayed the ER diagram for the COMPANY database schema. We discussed some of the basic concepts of UML class diagrams and how they relate to ER modeling concepts. We also described ternary and higher-degree relationship types in more detail, and we discussed the circumstances under which they are distinguished from binary relationships. Finally, we presented requirements for a UNIVERSITY database schema as another example, and we showed the ER schema design.

The ER modeling concepts we have presented thus far—entity types, relationship types, attributes, keys, and structural constraints—can model many database applications. However, more complex applications—such as engineering design, medical information systems, and telecommunications—require additional concepts if we want to model them with greater accuracy. We discuss some advanced modeling concepts in Chapter 8 and revisit further advanced data modeling techniques in Chapter 26.

## Review Questions

- 3.1. Discuss the role of a high-level data model in the database design process.
- 3.2. List the various cases where use of a NULL value would be appropriate.
- 3.3. Define the following terms: *entity*, *attribute*, *attribute value*, *relationship instance*, *composite attribute*, *multivalued attribute*, *derived attribute*, *complex attribute*, *key attribute*, and *value set (domain)*.
- 3.4. What is an entity type? What is an entity set? Explain the differences among an entity, an entity type, and an entity set.
- 3.5. Explain the difference between an attribute and a value set.
- 3.6. What is a relationship type? Explain the differences among a relationship instance, a relationship type, and a relationship set.
- 3.7. What is a participation role? When is it necessary to use role names in the description of relationship types?
- 3.8. Describe the two alternatives for specifying structural constraints on relationship types. What are the advantages and disadvantages of each?
- 3.9. Under what conditions can an attribute of a binary relationship type be migrated to become an attribute of one of the participating entity types?
- 3.10. When we think of relationships as attributes, what are the value sets of these attributes? What class of data models is based on this concept?
- 3.11. What is meant by a recursive relationship type? Give some examples of recursive relationship types.
- 3.12. When is the concept of a weak entity used in data modeling? Define the terms *owner entity type*, *weak entity type*, *identifying relationship type*, and *partial key*.
- 3.13. Can an identifying relationship of a weak entity type be of a degree greater than two? Give examples to illustrate your answer.
- 3.14. Discuss the conventions for displaying an ER schema as an ER diagram.
- 3.15. Discuss the naming conventions used for ER schema diagrams.

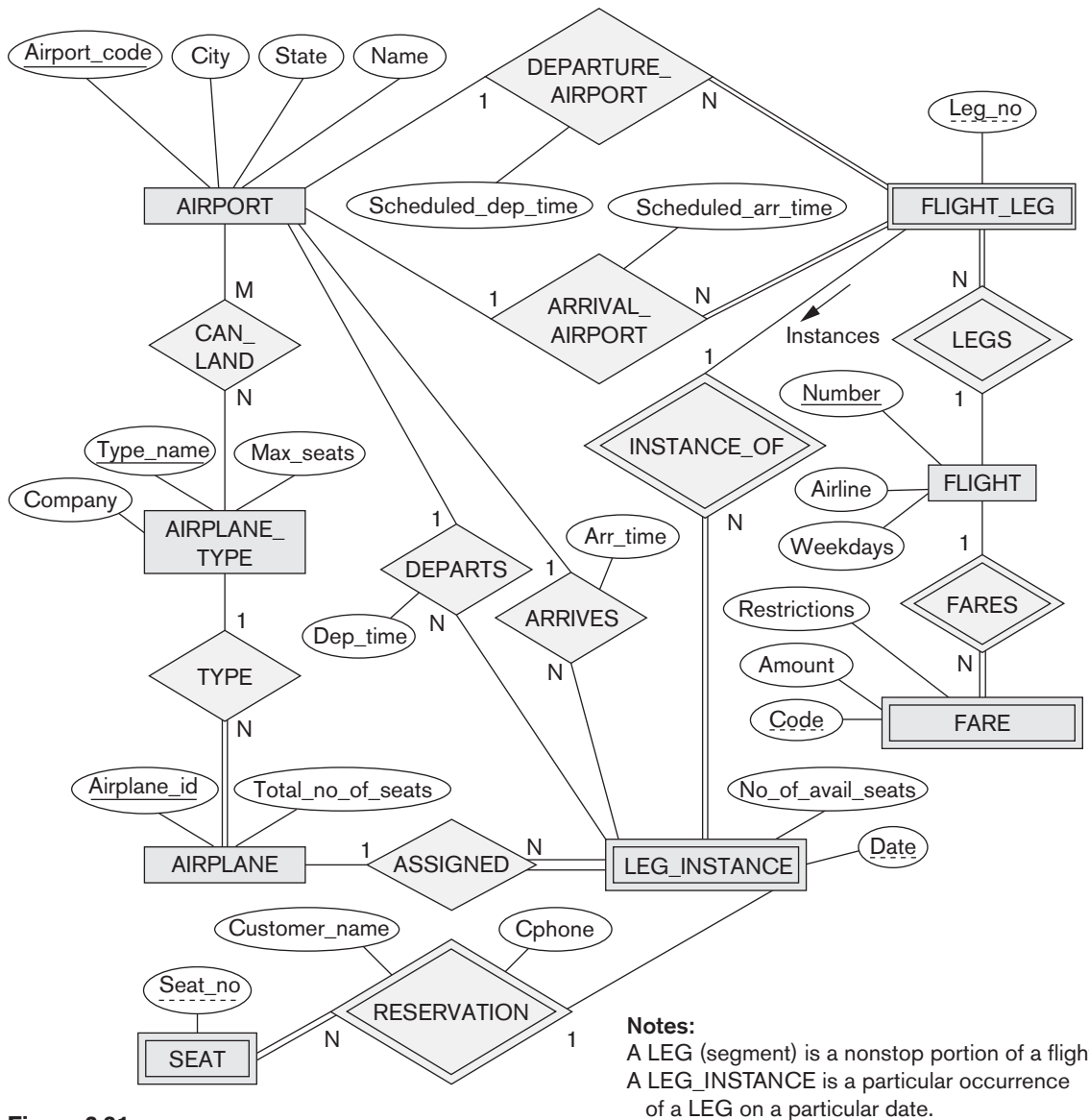
## Exercises

- 3.16. Which combinations of attributes have to be unique for each individual SECTION entity in the UNIVERSITY database shown in Figure 3.20 to enforce each of the following miniworld constraints:
  - a. During a particular semester and year, only one section can use a particular classroom at a particular DaysTime value.

- b. During a particular semester and year, an instructor can teach only one section at a particular DaysTime value.
- c. During a particular semester and year, the section numbers for sections offered for the same course must all be different.

Can you think of any other similar constraints?

- 3.17.** Composite and multivalued attributes can be nested to any number of levels. Suppose we want to design an attribute for a STUDENT entity type to keep track of previous college education. Such an attribute will have one entry for each college previously attended, and each such entry will be composed of college name, start and end dates, degree entries (degrees awarded at that college, if any), and transcript entries (courses completed at that college, if any). Each degree entry contains the degree name and the month and year the degree was awarded, and each transcript entry contains a course name, semester, year, and grade. Design an attribute to hold this information. Use the conventions in Figure 3.5.
- 3.18.** Show an alternative design for the attribute described in Exercise 3.17 that uses only entity types (including weak entity types, if needed) and relationship types.
- 3.19.** Consider the ER diagram in Figure 3.21, which shows a simplified schema for an airline reservations system. Extract from the ER diagram the requirements and constraints that produced this schema. Try to be as precise as possible in your requirements and constraints specification.
- 3.20.** In Chapters 1 and 2, we discussed the database environment and database users. We can consider many entity types to describe such an environment, such as DBMS, stored database, DBA, and catalog/data dictionary. Try to specify all the entity types that can fully describe a database system and its environment; then specify the relationship types among them, and draw an ER diagram to describe such a general database environment.
- 3.21.** Design an ER schema for keeping track of information about votes taken in the U.S. House of Representatives during the current two-year congressional session. The database needs to keep track of each U.S. STATE's Name (e.g., 'Texas', 'New York', 'California') and include the Region of the state (whose domain is {'Northeast', 'Midwest', 'Southeast', 'Southwest', 'West'}). Each CONGRESS\_PERSON in the House of Representatives is described by his or her Name, plus the District represented, the Start\_date when the congressperson was first elected, and the political Party to which he or she belongs (whose domain is {'Republican', 'Democrat', 'Independent', 'Other'}). The database keeps track of each BILL (i.e., proposed law), including the Bill\_name, the Date\_of\_vote on the bill, whether the bill Passed\_or\_failed (whose domain is {'Yes', 'No'}), and the Sponsor (the congressperson(s) who sponsored—that is, proposed—the bill). The database also keeps track of how each congressperson voted on each bill (domain



**Figure 3.21**  
 An ER diagram for an AIRLINE database schema.

of Vote attribute is {'Yes', 'No', 'Abstain', 'Absent'}). Draw an ER schema diagram for this application. State clearly any assumptions you make.

- 3.22.** A database is being constructed to keep track of the teams and games of a sports league. A team has a number of players, not all of whom participate in each game. It is desired to keep track of the players participating in each game for each team, the positions they played in that game, and the result of

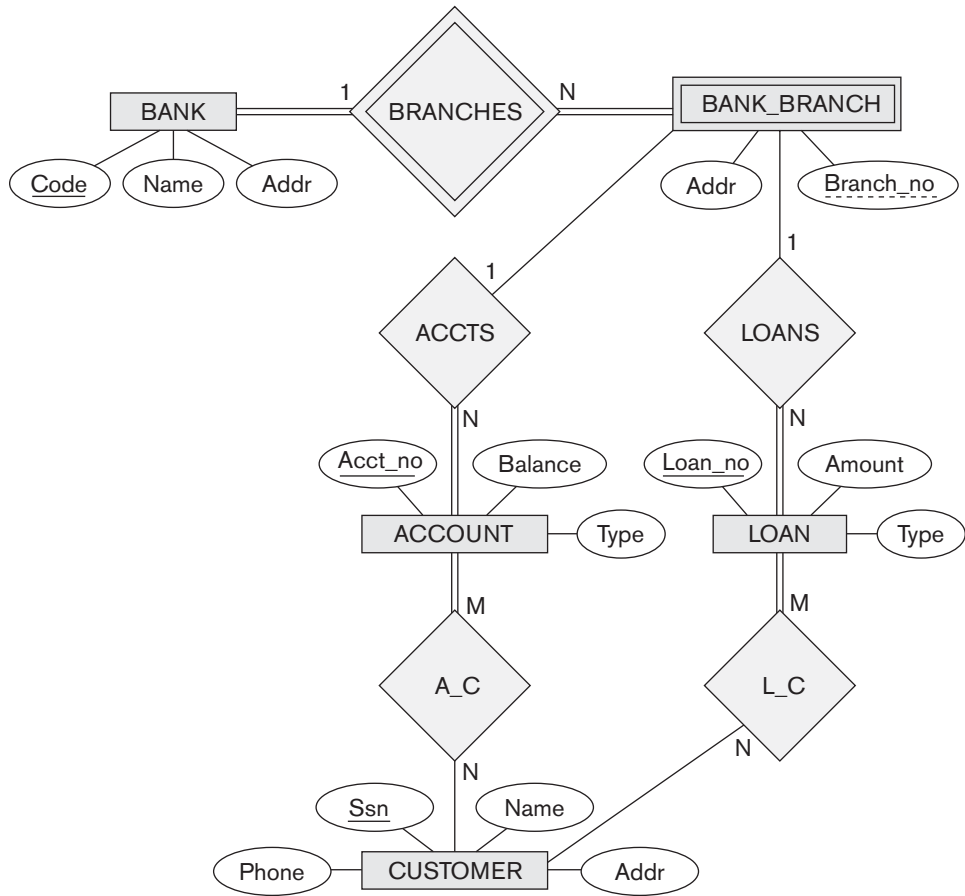


the game. Design an ER schema diagram for this application, stating any assumptions you make. Choose your favorite sport (e.g., soccer, baseball, football).

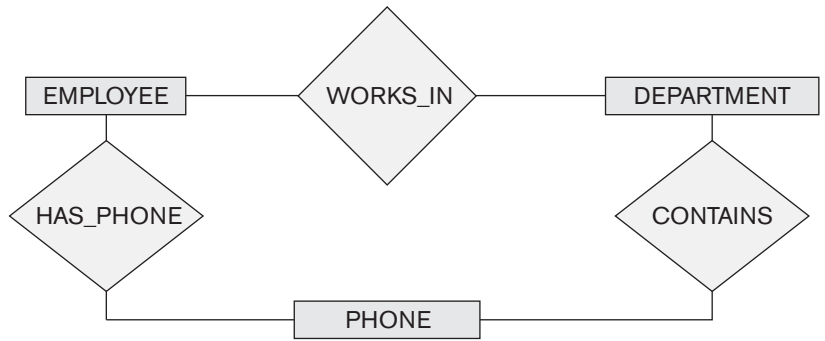
- 3.23. Consider the ER diagram shown in Figure 3.22 for part of a BANK database. Each bank can have multiple branches, and each branch can have multiple accounts and loans.
- List the strong (nonweak) entity types in the ER diagram.
  - Is there a weak entity type? If so, give its name, partial key, and identifying relationship.
  - What constraints do the partial key and the identifying relationship of the weak entity type specify in this diagram?
  - List the names of all relationship types, and specify the (min, max) constraint on each participation of an entity type in a relationship type. Justify your choices.

**Figure 3.22**

An ER diagram for a BANK database schema.

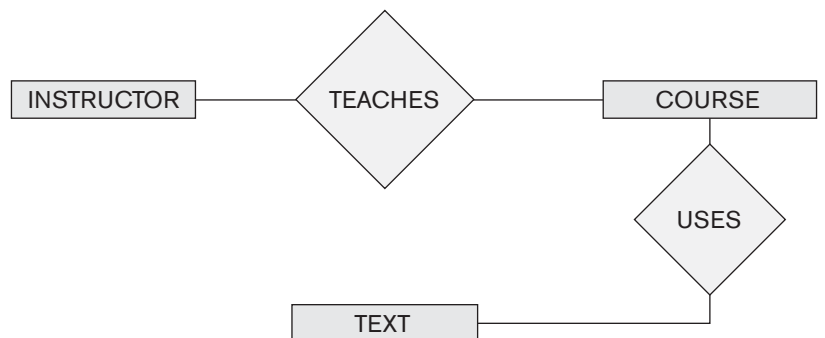


**Figure 3.23**  
Part of an ER diagram  
for a COMPANY  
database.



- e. List concisely the user requirements that led to this ER schema design.
- f. Suppose that every customer must have at least one account but is restricted to at most two loans at a time, and that a bank branch cannot have more than 1,000 loans. How does this show up on the (min, max) constraints?
- 3.24.** Consider the ER diagram in Figure 3.23. Assume that an employee may work in up to two departments or may not be assigned to any department. Assume that each department must have one and may have up to three phone numbers. Supply (min, max) constraints on this diagram. *State clearly any additional assumptions you make.* Under what conditions would the relationship HAS\_PHONE be redundant in this example?
- 3.25.** Consider the ER diagram in Figure 3.24. Assume that a course may or may not use a textbook, but that a text by definition is a book that is used in some course. A course may not use more than five books. Instructors teach from two to four courses. Supply (min, max) constraints on this diagram. *State clearly any additional assumptions you make.* If we add the relationship ADOPTS, to indicate the textbook(s) that an instructor uses for a course, should it be a binary relationship between INSTRUCTOR and TEXT, or a ternary relationship among all three entity types? What (min, max) constraints would you put on the relationship? Why?

**Figure 3.24**  
Part of an ER diagram  
for a COURSES  
database.



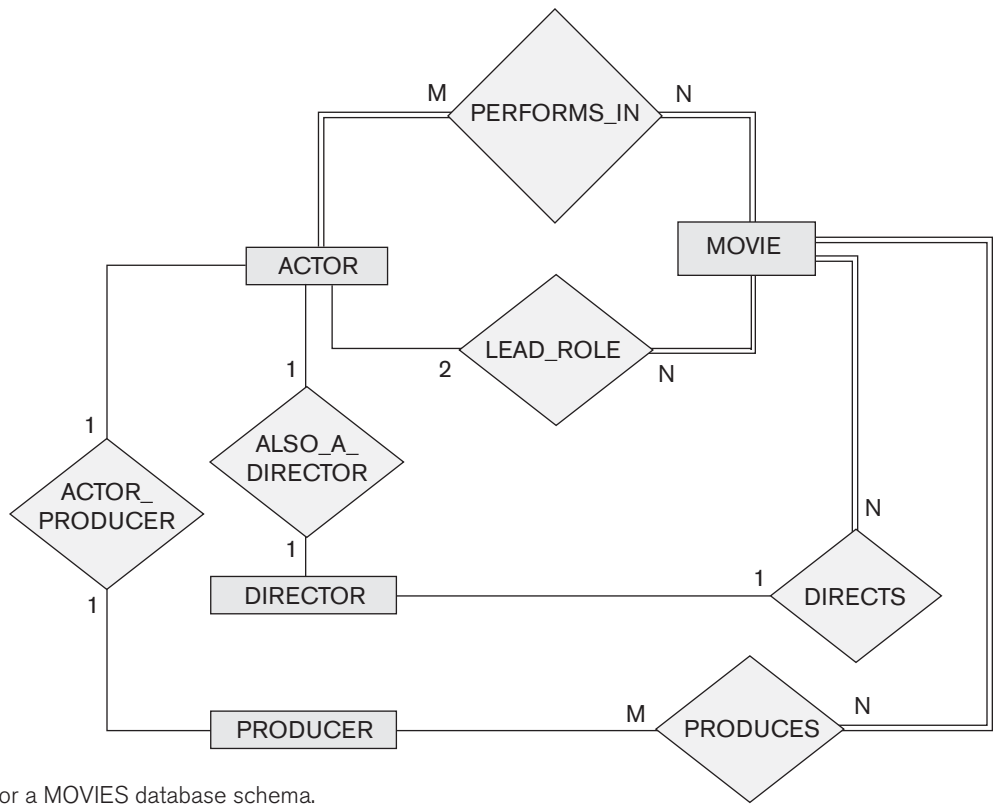
- 3.26. Consider an entity type SECTION in a UNIVERSITY database, which describes the section offerings of courses. The attributes of SECTION are Section\_number, Semester, Year, Course\_number, Instructor, Room\_no (where section is taught), Building (where section is taught), Weekdays (domain is the possible combinations of weekdays in which a section can be offered {'MWF', 'MW', 'TT', and so on}), and Hours (domain is all possible time periods during which sections are offered {'9–9:50 A.M.', '10–10:50 A.M.', . . . , '3:30–4:50 P.M.', '5:30–6:20 P.M.', and so on}). Assume that Section\_number is unique for each course within a particular semester/year combination (that is, if a course is offered multiple times during a particular semester, its section offerings are numbered 1, 2, 3, and so on). There are several composite keys for section, and some attributes are components of more than one key. Identify three composite keys, and show how they can be represented in an ER schema diagram.
- 3.27. Cardinality ratios often dictate the detailed design of a database. The cardinality ratio depends on the real-world meaning of the entity types involved and is defined by the specific application. For the following binary relationships, suggest cardinality ratios based on the common-sense meaning of the entity types. Clearly state any assumptions you make.

Entity 1	Cardinality Ratio	Entity 2
1. STUDENT	_____	SOCIAL_SECURITY_CARD
2. STUDENT	_____	TEACHER
3. CLASSROOM	_____	WALL
4. COUNTRY	_____	CURRENT_PRESIDENT
5. COURSE	_____	TEXTBOOK
6. ITEM (that can be found in an order)	_____	ORDER
7. STUDENT	_____	CLASS
8. CLASS	_____	INSTRUCTOR
9. INSTRUCTOR	_____	OFFICE
10. EBAY_AUCTION_ITEM	_____	EBAY_BID

- 3.28. Consider the ER schema for the MOVIES database in Figure 3.25.

Assume that MOVIES is a populated database. ACTOR is used as a generic term and includes actresses. Given the constraints shown in the ER schema, respond to the following statements with *True*, *False*, or *Maybe*. Assign a response of *Maybe* to statements that, although not explicitly shown to be *True*, cannot be proven *False* based on the schema as shown. Justify each answer.

- There are no actors in this database that have been in no movies.
- There are some actors who have acted in more than ten movies.
- Some actors have done a lead role in multiple movies.
- A movie can have only a maximum of two lead actors.



**Figure 3.25**  
An ER diagram for a MOVIES database schema.

- e. Every director has been an actor in some movie.
  - f. No producer has ever been an actor.
  - g. A producer cannot be an actor in some other movie.
  - h. There are movies with more than a dozen actors.
  - i. Some producers have been a director as well.
  - j. Most movies have one director and one producer.
  - k. Some movies have one director but several producers.
  - l. There are some actors who have done a lead role, directed a movie, and produced a movie.
  - m. No movie has a director who also acted in that movie.
- 3.29.** Given the ER schema for the MOVIES database in Figure 3.25, draw an instance diagram using three movies that have been released recently. Draw instances of each entity type: MOVIES, ACTORS, PRODUCERS, DIRECTORS involved; make up instances of the relationships as they exist in reality for those movies.

- 3.30.** Illustrate the UML diagram for Exercise 3.16. Your UML design should observe the following requirements:
- A student should have the ability to compute his/her GPA and add or drop majors and minors.
  - Each department should be able to add or delete courses and hire or terminate faculty.
  - Each instructor should be able to assign or change a student's grade for a course.

*Note:* Some of these functions may be spread over multiple classes.

## Laboratory Exercises

- 3.31.** Consider the UNIVERSITY database described in Exercise 3.16. Build the ER schema for this database using a data modeling tool such as ERwin or Rational Rose.
- 3.32.** Consider a MAIL\_ORDER database in which employees take orders for parts from customers. The data requirements are summarized as follows:
- The mail order company has employees, each identified by a unique employee number, first and last name, and Zip Code.
  - Each customer of the company is identified by a unique customer number, first and last name, and Zip Code.
  - Each part sold by the company is identified by a unique part number, a part name, price, and quantity in stock.
  - Each order placed by a customer is taken by an employee and is given a unique order number. Each order contains specified quantities of one or more parts. Each order has a date of receipt as well as an expected ship date. The actual ship date is also recorded.

Design an entity–relationship diagram for the mail order database and build the design using a data modeling tool such as ERwin or Rational Rose.

- 3.33.** Consider a MOVIE database in which data is recorded about the movie industry. The data requirements are summarized as follows:
- Each movie is identified by title and year of release. Each movie has a length in minutes. Each has a production company, and each is classified under one or more genres (such as horror, action, drama, and so forth). Each movie has one or more directors and one or more actors appear in it. Each movie also has a plot outline. Finally, each movie has zero or more quotable quotes, each of which is spoken by a particular actor appearing in the movie.
  - Actors are identified by name and date of birth and appear in one or more movies. Each actor has a role in the movie.

- Directors are also identified by name and date of birth and direct one or more movies. It is possible for a director to act in a movie (including one that he or she may also direct).
- Production companies are identified by name and each has an address. A production company produces one or more movies.

Design an entity–relationship diagram for the movie database and enter the design using a data modeling tool such as ERwin or Rational Rose.

**3.34.** Consider a CONFERENCE\_REVIEW database in which researchers submit their research papers for consideration. Reviews by reviewers are recorded for use in the paper selection process. The database system caters primarily to reviewers who record answers to evaluation questions for each paper they review and make recommendations regarding whether to accept or reject the paper. The data requirements are summarized as follows:

- Authors of papers are uniquely identified by e-mail id. First and last names are also recorded.
- Each paper is assigned a unique identifier by the system and is described by a title, abstract, and the name of the electronic file containing the paper.
- A paper may have multiple authors, but one of the authors is designated as the contact author.
- Reviewers of papers are uniquely identified by e-mail address. Each reviewer’s first name, last name, phone number, affiliation, and topics of interest are also recorded.
- Each paper is assigned between two and four reviewers. A reviewer rates each paper assigned to him or her on a scale of 1 to 10 in four categories: technical merit, readability, originality, and relevance to the conference. Finally, each reviewer provides an overall recommendation regarding each paper.
- Each review contains two types of written comments: one to be seen by the review committee only and the other as feedback to the author(s).

Design an entity–relationship diagram for the CONFERENCE\_REVIEW database and build the design using a data modeling tool such as ERwin or Rational Rose.

**3.35.** Consider the ER diagram for the AIRLINE database shown in Figure 3.21. Build this design using a data modeling tool such as ERwin or Rational Rose.

## Selected Bibliography

The entity–relationship model was introduced by Chen (1976), and related work appears in Schmidt and Swenson (1975), Wiederhold and Elmasri (1979), and Senko (1975). Since then, numerous modifications to the ER model have been suggested. We have incorporated some of these in our presentation. Structural

constraints on relationships are discussed in Abrial (1974), Elmasri and Wiederhold (1980), and Lenzerini and Santucci (1983). Multivalued and composite attributes are incorporated in the ER model in Elmasri et al. (1985). Although we did not discuss languages for the ER model and its extensions, there have been several proposals for such languages. Elmasri and Wiederhold (1981) proposed the GORDAS query language for the ER model. Another ER query language was proposed by Markowitz and Raz (1983). Senko (1980) presented a query language for Senko's DIAM model. A formal set of operations called the ER algebra was presented by Parent and Spaccapietra (1985). Gogolla and Hohenstein (1991) presented another formal language for the ER model. Campbell et al. (1985) presented a set of ER operations and showed that they are relationally complete. A conference for the dissemination of research results related to the ER model has been held regularly since 1979. The conference, now known as the International Conference on Conceptual Modeling, has been held in Los Angeles (ER 1979, ER 1983, ER 1997), Washington, D.C. (ER 1981), Chicago (ER 1985), Dijon, France (ER 1986), New York City (ER 1987), Rome (ER 1988), Toronto (ER 1989), Lausanne, Switzerland (ER 1990), San Mateo, California (ER 1991), Karlsruhe, Germany (ER 1992), Arlington, Texas (ER 1993), Manchester, England (ER 1994), Brisbane, Australia (ER 1995), Cottbus, Germany (ER 1996), Singapore (ER 1998), Paris, France (ER 1999), Salt Lake City, Utah (ER 2000), Yokohama, Japan (ER 2001), Tampere, Finland (ER 2002), Chicago, Illinois (ER 2003), Shanghai, China (ER 2004), Klagenfurt, Austria (ER 2005), Tucson, Arizona (ER 2006), Auckland, New Zealand (ER 2007), Barcelona, Catalonia, Spain (ER 2008), and Gramado, RS, Brazil (ER 2009). The 2010 conference was held in Vancouver, British Columbia, Canada (ER2010), 2011 in Brussels, Belgium (ER2011), 2012 in Florence, Italy (ER2012), 2013 in Hong Kong, China (ER2013), and the 2014 conference was held in Atlanta, Georgia (ER 2014). The 2015 conference is to be held in Stockholm, Sweden.

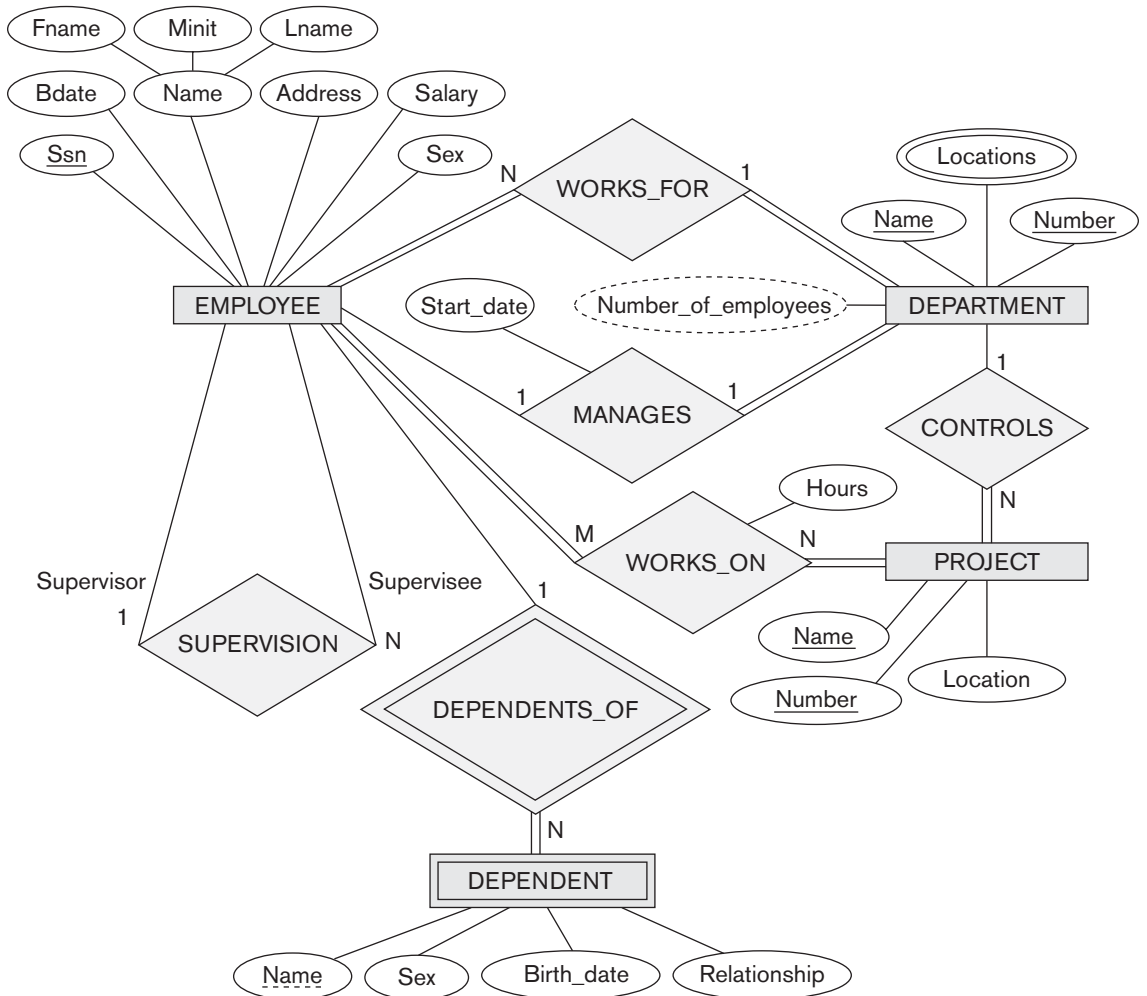
# 9.1 Relational Database Design Using ER-to-Relational Mapping

## 9.1.1 ER-to-Relational Mapping Algorithm

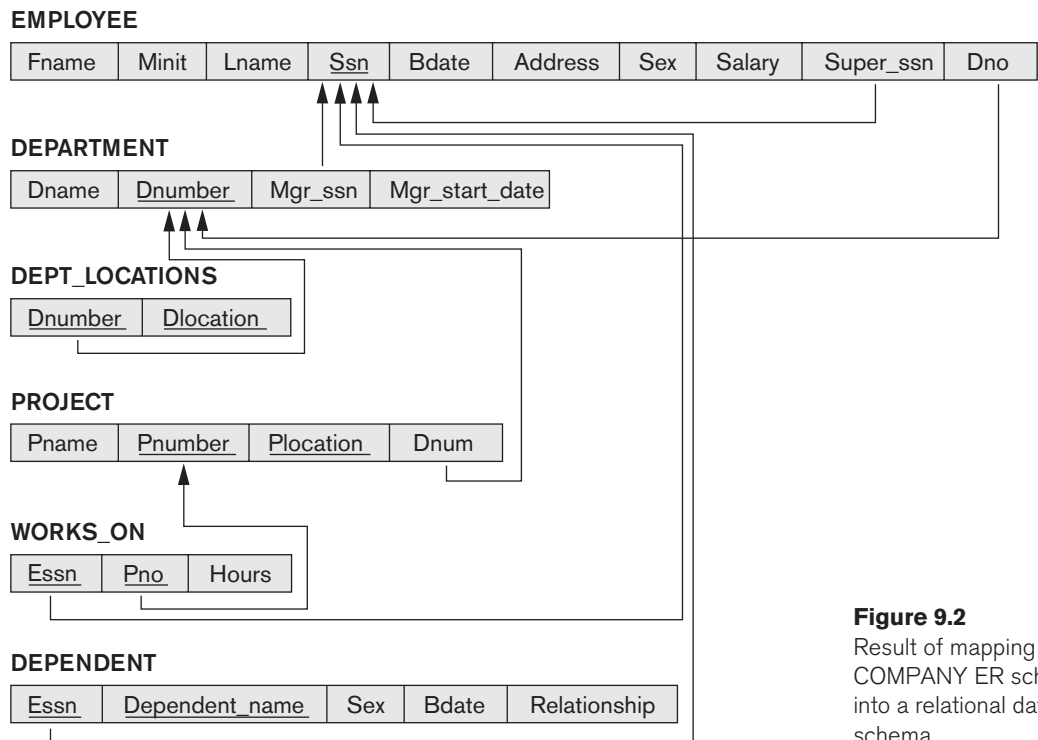
In this section we describe the steps of an algorithm for ER-to-relational mapping. We use the COMPANY database example to illustrate the mapping procedure. The COMPANY ER schema is shown again in Figure 9.1, and the corresponding COMPANY relational database schema is shown in Figure 9.2 to illustrate the the

**Figure 9.1**

The ER conceptual schema diagram for the COMPANY database.







**Figure 9.2**  
Result of mapping the  
COMPANY ER schema  
into a relational data  
schema.

mapping steps. We assume that the mapping will create tables with simple single-valued attributes. The relational model constraints defined in Chapter 5, which include primary keys, unique keys (if any), and referential integrity constraints on the relations, will also be specified in the mapping results.

**Step 1: Mapping of Regular Entity Types.** For each regular (strong) entity type  $E$  in the ER schema, create a relation  $R$  that includes all the simple attributes of  $E$ . Include only the simple component attributes of a composite attribute. Choose one of the key attributes of  $E$  as the primary key for  $R$ . If the chosen key of  $E$  is a composite, then the set of simple attributes that form it will together form the primary key of  $R$ .

If multiple keys were identified for  $E$  during the conceptual design, the information describing the attributes that form each additional key is kept in order to specify additional (unique) keys of relation  $R$ . Knowledge about keys is also kept for indexing purposes and other types of analyses.

In our example, we create the relations EMPLOYEE, DEPARTMENT, and PROJECT in Figure 9.2 to correspond to the regular entity types EMPLOYEE, DEPARTMENT, and PROJECT from Figure 9.1. The foreign key and relationship attributes, if any, are not included yet; they will be added during subsequent steps. These include

the attributes Super\_ssn and Dno of EMPLOYEE, Mgr\_ssn and Mgr\_start\_date of DEPARTMENT, and Dnum of PROJECT. In our example, we choose Ssn, Dnumber, and Pnumber as primary keys for the relations EMPLOYEE, DEPARTMENT, and PROJECT, respectively. Knowledge that Dname of DEPARTMENT and Pname of PROJECT are unique keys is kept for possible use later in the design.

The relations that are created from the mapping of entity types are sometimes called **entity relations** because each tuple represents an entity instance. The result after this mapping step is shown in Figure 9.3(a).

**Step 2: Mapping of Weak Entity Types.** For each weak entity type  $W$  in the ER schema with owner entity type  $E$ , create a relation  $R$  and include all simple attributes (or simple components of composite attributes) of  $W$  as attributes of  $R$ . In addition, include as foreign key attributes of  $R$ , the primary key attribute(s) of the relation(s) that correspond to the owner entity type(s); this takes care of mapping the identifying relationship type of  $W$ . The primary key of  $R$  is the combination of the primary key(s) of the owner(s) and the partial key of the weak entity type  $W$ , if any. If there is a weak entity type  $E_2$  whose owner is also a weak entity type  $E_1$ , then  $E_1$  should be mapped before  $E_2$  to determine its primary key first.

In our example, we create the relation DEPENDENT in this step to correspond to the weak entity type DEPENDENT (see Figure 9.3(b)). We include the primary key Ssn of the EMPLOYEE relation—which corresponds to the owner entity type—as a foreign key attribute of DEPENDENT; we rename it Essn, although this is not

**Figure 9.3**

Illustration of some mapping steps.

(a) *Entity* relations after step 1.

(b) Additional *weak entity* relation after step 2.

(c) *Relationship* relations after step 5.

(d) Relation representing multivalued attribute after step 6.

(a) **EMPLOYEE**

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary
-------	-------	-------	------------	-------	---------	-----	--------

**DEPARTMENT**

Dname	<u>Dnumber</u>
-------	----------------

**PROJECT**

Pname	<u>Pnumber</u>	Plocation
-------	----------------	-----------

(b) **DEPENDENT**

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
-------------	-----------------------	-----	-------	--------------

(c) **WORKS\_ON**

<u>Essn</u>	<u>Pno</u>	Hours
-------------	------------	-------

(d) **DEPT\_LOCATIONS**

<u>Dnumber</u>	<u>Dlocation</u>
----------------	------------------

necessary. The primary key of the DEPENDENT relation is the combination {Essn, Dependent\_name}, because Dependent\_name (also renamed from Name in Figure 9.1) is the partial key of DEPENDENT.

It is common to choose the propagate (CASCADE) option for the referential triggered action (see Section 6.2) on the foreign key in the relation corresponding to the weak entity type, since a weak entity has an existence dependency on its owner entity. This can be used for both ON UPDATE and ON DELETE.

**Step 3: Mapping of Binary 1:1 Relationship Types.** For each binary 1:1 relationship type  $R$  in the ER schema, identify the relations  $S$  and  $T$  that correspond to the entity types participating in  $R$ . There are three possible approaches: (1) the foreign key approach, (2) the merged relationship approach, and (3) the cross-reference or relationship relation approach. The first approach is the most useful and should be followed unless special conditions exist, as we discuss below.

1. **Foreign key approach:** Choose one of the relations— $S$ , say—and include as a foreign key in  $S$  the primary key of  $T$ . It is better to choose an entity type with *total participation* in  $R$  in the role of  $S$ . Include all the simple attributes (or simple components of composite attributes) of the 1:1 relationship type  $R$  as attributes of  $S$ .

In our example, we map the 1:1 relationship type MANAGES from Figure 9.1 by choosing the participating entity type DEPARTMENT to serve in the role of  $S$  because its participation in the MANAGES relationship type is total (every department has a manager). We include the primary key of the EMPLOYEE relation as foreign key in the DEPARTMENT relation and rename it to Mgr\_ssn. We also include the simple attribute Start\_date of the MANAGES relationship type in the DEPARTMENT relation and rename it Mgr\_start\_date (see Figure 9.2).

Note that it is possible to include the primary key of  $S$  as a foreign key in  $T$  instead. In our example, this amounts to having a foreign key attribute, say Department\_managed in the EMPLOYEE relation, but it will have a NULL value for employee tuples who do not manage a department. This would be a bad choice, because if only 2% of employees manage a department, then 98% of the foreign keys would be NULL in this case. Another possibility is to have foreign keys in both relations  $S$  and  $T$  redundantly, but this creates redundancy and incurs a penalty for consistency maintenance.

2. **Merged relation approach:** An alternative mapping of a 1:1 relationship type is to merge the two entity types and the relationship into a single relation. This is possible when *both participations are total*, as this would indicate that the two tables will have the exact same number of tuples at all times.
3. **Cross-reference or relationship relation approach:** The third option is to set up a third relation  $R$  for the purpose of cross-referencing the primary keys of the two relations  $S$  and  $T$  representing the entity types. As we will see, this approach is required for binary M:N relationships. The relation  $R$  is called a **relationship relation** (or sometimes a **lookup table**), because each

tuple in  $R$  represents a relationship instance that relates one tuple from  $S$  with one tuple from  $T$ . The relation  $R$  will include the primary key attributes of  $S$  and  $T$  as foreign keys to  $S$  and  $T$ . The primary key of  $R$  will be one of the two foreign keys, and the other foreign key will be a unique key of  $R$ . The drawback is having an extra relation, and requiring extra join operations when combining related tuples from the tables.

**Step 4: Mapping of Binary 1:N Relationship Types.** There are two possible approaches: (1) the foreign key approach and (2) the cross-reference or relationship relation approach. The first approach is generally preferred as it reduces the number of tables.

1. **The foreign key approach:** For each regular binary 1:N relationship type  $R$ , identify the relation  $S$  that represents the participating entity type at the  $N$ -side of the relationship type. Include as foreign key in  $S$  the primary key of the relation  $T$  that represents the other entity type participating in  $R$ ; we do this because each entity instance on the  $N$ -side is related to at most one entity instance on the 1-side of the relationship type. Include any simple attributes (or simple components of composite attributes) of the 1:N relationship type as attributes of  $S$ .

To apply this approach to our example, we map the 1:N relationship types WORKS\_FOR, CONTROLS, and SUPERVISION from Figure 9.1. For WORKS\_FOR we include the primary key Dnumber of the DEPARTMENT relation as foreign key in the EMPLOYEE relation and call it Dno. For SUPERVISION we include the primary key of the EMPLOYEE relation as foreign key in the EMPLOYEE relation itself—because the relationship is recursive—and call it Super\_ssn. The CONTROLS relationship is mapped to the foreign key attribute Dnum of PROJECT, which references the primary key Dnumber of the DEPARTMENT relation. These foreign keys are shown in Figure 9.2.

2. **The relationship relation approach:** An alternative approach is to use the **relationship relation** (cross-reference) option as in the third option for binary 1:1 relationships. We create a separate relation  $R$  whose attributes are the primary keys of  $S$  and  $T$ , which will also be foreign keys to  $S$  and  $T$ . The primary key of  $R$  is the same as the primary key of  $S$ . This option can be used if few tuples in  $S$  participate in the relationship to avoid excessive NULL values in the foreign key.

**Step 5: Mapping of Binary M:N Relationship Types.** In the traditional relational model with no multivalued attributes, the only option for M:N relationships is the **relationship relation (cross-reference) option**. For each binary M:N relationship type  $R$ , create a new relation  $S$  to represent  $R$ . Include as foreign key attributes in  $S$  the primary keys of the relations that represent the participating entity types; their *combination* will form the primary key of  $S$ . Also include any simple attributes of the M:N relationship type (or simple components of composite attributes) as attributes of  $S$ . Notice that we cannot represent an M:N relationship type by a single foreign key attribute in one of the participating relations (as we did for

1:1 or 1:N relationship types) because of the M:N cardinality ratio; we must create a separate *relationship relation* *S*.

In our example, we map the M:N relationship type WORKS\_ON from Figure 9.1 by creating the relation WORKS\_ON in Figure 9.2. We include the primary keys of the PROJECT and EMPLOYEE relations as foreign keys in WORKS\_ON and rename them Pno and Essn, respectively (renaming is *not required*; it is a design choice). We also include an attribute Hours in WORKS\_ON to represent the Hours attribute of the relationship type. The primary key of the WORKS\_ON relation is the combination of the foreign key attributes {Essn, Pno}. This **relationship relation** is shown in Figure 9.3(c).

The propagate (CASCADE) option for the referential triggered action (see Section 4.2) should be specified on the foreign keys in the relation corresponding to the relationship *R*, since each relationship instance has an existence dependency on each of the entities it relates. This can be used for both ON UPDATE and ON DELETE.

Although we can map 1:1 or 1:N relationships in a manner similar to M:N relationships by using the cross-reference (relationship relation) approach, as we discussed earlier, this is only recommended when few relationship instances exist, in order to avoid NULL values in foreign keys. In this case, the primary key of the relationship relation will be *only one* of the foreign keys that reference the participating entity relations. For a 1:N relationship, the primary key of the relationship relation will be the foreign key that references the entity relation on the N-side. For a 1:1 relationship, either foreign key can be used as the primary key of the relationship relation.

**Step 6: Mapping of Multivalued Attributes.** For each multivalued attribute *A*, create a new relation *R*. This relation *R* will include an attribute corresponding to *A*, plus the primary key attribute *K*—as a foreign key in *R*—of the relation that represents the entity type or relationship type that has *A* as a multivalued attribute. The primary key of *R* is the combination of *A* and *K*. If the multivalued attribute is composite, we include its simple components.

In our example, we create a relation DEPT\_LOCATIONS (see Figure 9.3(d)). The attribute Dlocation represents the multivalued attribute LOCATIONS of DEPARTMENT, whereas Dnumber—as foreign key—represents the primary key of the DEPARTMENT relation. The primary key of DEPT\_LOCATIONS is the combination of {Dnumber, Dlocation}. A separate tuple will exist in DEPT\_LOCATIONS for each location that a department has. It is important to note that in more recent versions of the relational model that allow array data types, the multivalued attribute can be mapped to an array attribute rather than requiring a separate table.

The propagate (CASCADE) option for the referential triggered action (see Section 6.2) should be specified on the foreign key in the relation *R* corresponding to the multivalued attribute for both ON UPDATE and ON DELETE. We should also note that the key of *R* when mapping a composite, multivalued attribute requires some analysis of the meaning of the component attributes. In some cases, when a multivalued attribute is composite, only some of the component attributes are required

to be part of the key of  $R$ ; these attributes are similar to a partial key of a weak entity type that corresponds to the multivalued attribute (see Section 3.5).

Figure 9.2 shows the COMPANY relational database schema obtained with steps 1 through 6, and Figure 5.6 shows a sample database state. Notice that we did not yet discuss the mapping of  $n$ -ary relationship types ( $n > 2$ ) because none exist in Figure 9.1; these are mapped in a similar way to M:N relationship types by including the following additional step in the mapping algorithm.

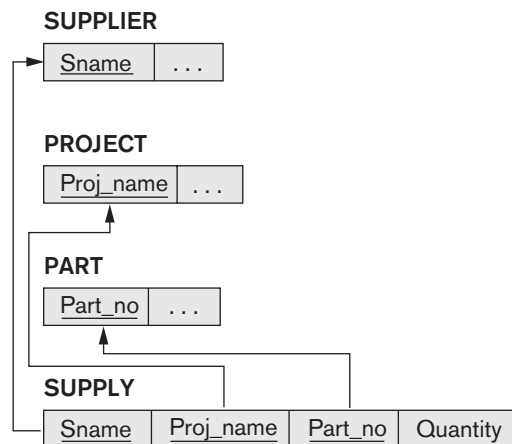
**Step 7: Mapping of  $N$ -ary Relationship Types.** We use the **relationship relation option**. For each  $n$ -ary relationship type  $R$ , where  $n > 2$ , create a new relationship relation  $S$  to represent  $R$ . Include as foreign key attributes in  $S$  the primary keys of the relations that represent the participating entity types. Also include any simple attributes of the  $n$ -ary relationship type (or simple components of composite attributes) as attributes of  $S$ . The primary key of  $S$  is usually a combination of all the foreign keys that reference the relations representing the participating entity types. However, if the cardinality constraints on any of the entity types  $E$  participating in  $R$  is 1, then the primary key of  $S$  should not include the foreign key attribute that references the relation  $E'$  corresponding to  $E$  (see the discussion in Section 3.9.2 concerning constraints on  $n$ -ary relationships).

Consider the ternary relationship type SUPPLY in Figure 3.17, which relates a SUPPLIER  $s$ , PART  $p$ , and PROJECT  $j$  whenever  $s$  is currently supplying  $p$  to  $j$ ; this can be mapped to the relation SUPPLY shown in Figure 9.4, whose primary key is the combination of the three foreign keys {Sname, Part\_no, Proj\_name}.

## 9.1.2 Discussion and Summary of Mapping for ER Model Constructs

Table 9.1 summarizes the correspondences between ER and relational model constructs and constraints.

**Figure 9.4**  
Mapping the  $n$ -ary relationship type SUPPLY from Figure 3.17(a).



**Table 9.1** Correspondence between ER and Relational Models

ER MODEL	RELATIONAL MODEL
Entity type	<i>Entity</i> relation
1:1 or 1:N relationship type	Foreign key (or <i>relationship</i> relation)
M:N relationship type	<i>Relationship</i> relation and <i>two</i> foreign keys
<i>n</i> -ary relationship type	<i>Relationship</i> relation and <i>n</i> foreign keys
Simple attribute	Attribute
Composite attribute	Set of simple component attributes
Multivalued attribute	Relation and foreign key
Value set	Domain
Key attribute	Primary (or secondary) key

One of the main points to note in a relational schema, in contrast to an ER schema, is that relationship types are not represented explicitly; instead, they are represented by having two attributes *A* and *B*, one a primary key and the other a foreign key (over the same domain) included in two relations *S* and *T*. Two tuples in *S* and *T* are related when they have the same value for *A* and *B*. By using the EQUIJOIN operation (or NATURAL JOIN if the two join attributes have the same name) over *S.A* and *T.B*, we can combine all pairs of related tuples from *S* and *T* and materialize the relationship. When a binary 1:1 or 1:N relationship type is involved and the foreign key mapping is used, a single join operation is usually needed. When the relationship relation approach is used, such as for a binary M:N relationship type, two join operations are needed, whereas for *n*-ary relationship types, *n* joins are needed to fully materialize the relationship instances.

For example, to form a relation that includes the employee name, project name, and hours that the employee works on each project, we need to connect each EMPLOYEE tuple to the related PROJECT tuples via the WORKS\_ON relation in Figure 9.2. Hence, we must apply the EQUIJOIN operation to the EMPLOYEE and WORKS\_ON relations with the join condition EMPLOYEE.Ssn = WORKS\_ON.Essn, and then apply another EQUIJOIN operation to the resulting relation and the PROJECT relation with join condition WORKS\_ON.Pno = PROJECT.Pnumber. In general, when multiple relationships need to be traversed, numerous join operations must be specified. The user must always be aware of the foreign key attributes in order to use them correctly in combining related tuples from two or more relations. This is sometimes considered to be a drawback of the relational data model, because the foreign key/primary key correspondences are not always obvious upon inspection of relational schemas. If an EQUIJOIN is performed among attributes of two relations that do not represent a foreign key/primary key relationship, the result can often be meaningless and may lead to spurious data. For example, the reader can try joining the PROJECT and DEPT\_LOCATIONS relations on the condition Dlocation = Plocation and examine the result.

In the relational schema we create a separate relation for *each* multivalued attribute. For a particular entity with a set of values for the multivalued attribute, the key attribute value of the entity is repeated once for each value of the multivalued attribute in a separate tuple because the basic relational model does *not* allow multiple values (a list, or a set of values) for an attribute in a single tuple. For example, because department 5 has three locations, three tuples exist in the DEPT\_LOCATIONS relation in Figure 3.6; each tuple specifies one of the locations. In our example, we apply EQUIJOIN to DEPT\_LOCATIONS and DEPARTMENT on the Dnumber attribute to get the values of all locations along with other DEPARTMENT attributes. In the resulting relation, the values of the other DEPARTMENT attributes are repeated in separate tuples for every location that a department has.

The basic relational algebra does not have a NEST or COMPRESS operation that would produce a set of tuples of the form {<'1', 'Houston'>, <'4', 'Stafford'>, <'5', {'Bellaire', 'Sugarland', 'Houston'}>} from the DEPT\_LOCATIONS relation in Figure 3.6. This is a serious drawback of the basic normalized or *flat* version of the relational model. The object data model and object-relational systems (see Chapter 12) do allow multivalued attributes by using the array type for the attribute.